

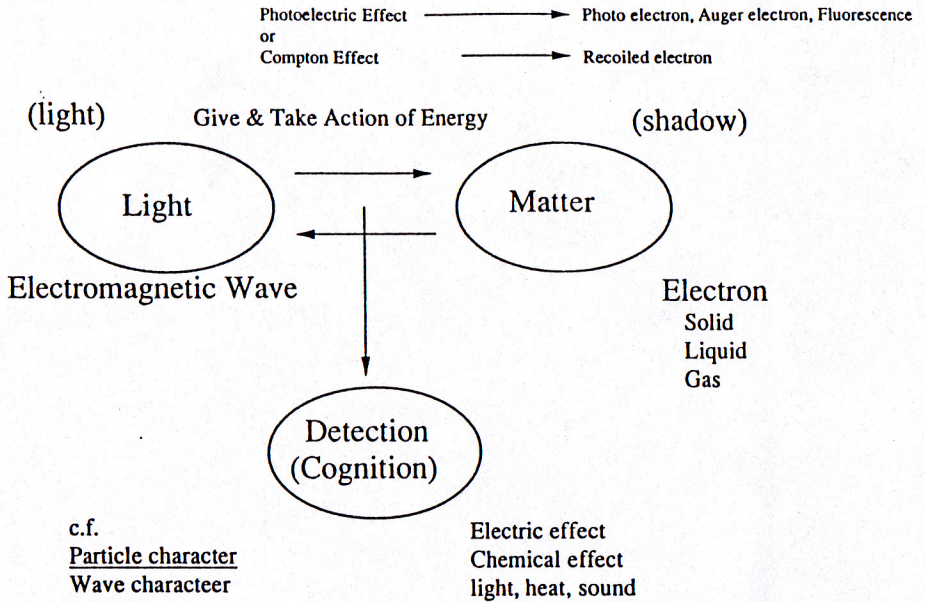
Contents of the Lecture on "Detectors"  
by Y. Amemiya ( Univ. of Tokyo)

- 1 Principle of X-ray Detection
- 2 Statistics Relating with X-ray Detection
- 3 Requirements for X-ray Detectors for Use with SR
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  - Linearity of Response
  - Detective Quantum Efficiency (DQE)
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JASS'02 at Amman  
October 19 – 28, 2002

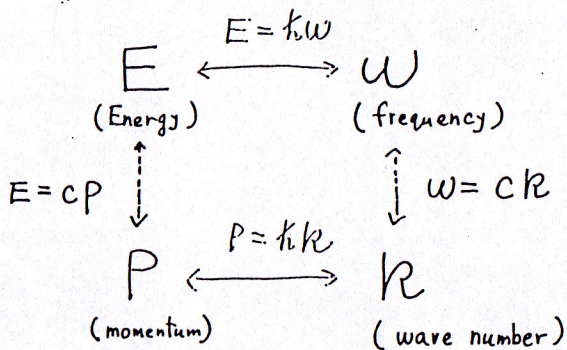
Yoshiyuki Amemiya  
Univ. of Tokyo, Japan

X-ray Detectors for Use with Synchrotron Radiation



Particle character

Wave character



Detector

E: energy  
P: position (direction)  
t: time

Analyzer

$\sim 10^{18}$  Hz  
phase ... coherency  
polarization

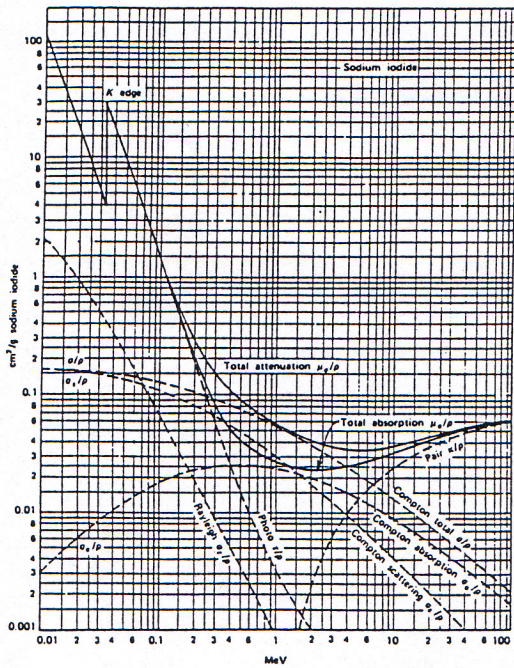
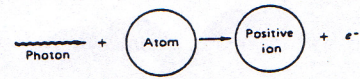
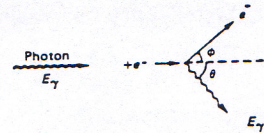


Figure 2-18 Energy dependence of the various gamma-ray interaction processes in sodium iodide. (From *The Atomic Nucleus* by R. D. Evans. Copyright 1955 by the McGraw-Hill Book Company. Used with permission.)



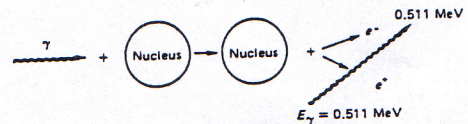
The photoelectric effect.

光電効果



The Compton effect.

コンプトン効果



Pair production. The gamma disappears and a positron-electron pair is created. Two 0.511-MeV photons are produced when the positron annihilates.

電子対生成

## Binomial Distribution

$P$ : success probability

$1-P$ : otherwise (failure probability)

$$P(x) = \frac{n!}{(n-x)! x!} P^x (1-P)^{n-x}$$

↑  
probability of counting exactly  $x$  successes for  $n$  trials.

Assumption: success probability ( $P$ ) is a constant.  
                  "                  each trial is independent

When

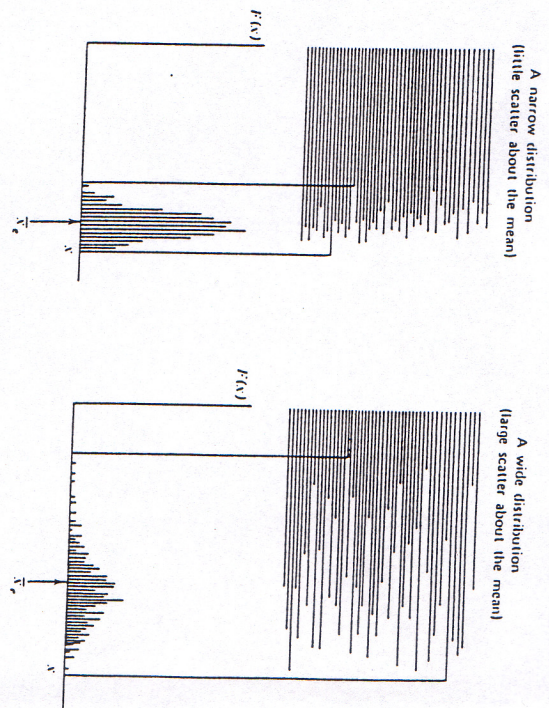
$$P \ll 1$$

$$Pn = m = \text{constant}$$



Poisson Distribution

Figure 3-2 Distribution functions for two sets of data with differing amounts of internal fluctuation.



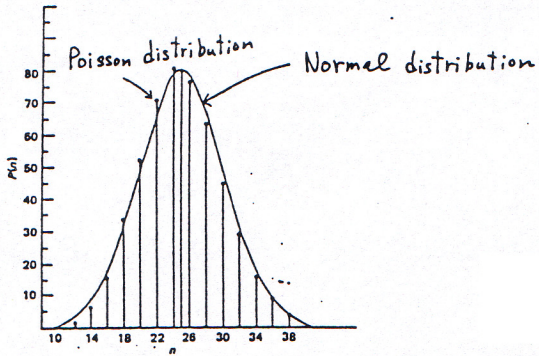
When,  $m(\text{average}) \geq 20$

Poisson distribution  $\approx$  Normal distribution

average =  $m$

variance =  $m$

(S.D. =  $\sqrt{m}$ )



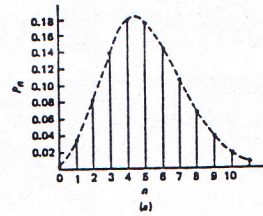
Comparison between a Poisson distribution with  $m = 25$  and a Gaussian distribution with the same average and standard deviation  $\sigma = \sqrt{m} = 5$ .

## Poisson Distribution

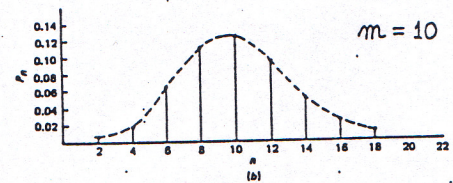
$$P(m) = \frac{m^n}{n!} e^{-m}$$

average =  $m$

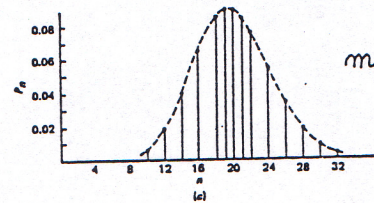
standard deviation =  $\sqrt{m}$  (variance =  $m$ )



$m = 5$



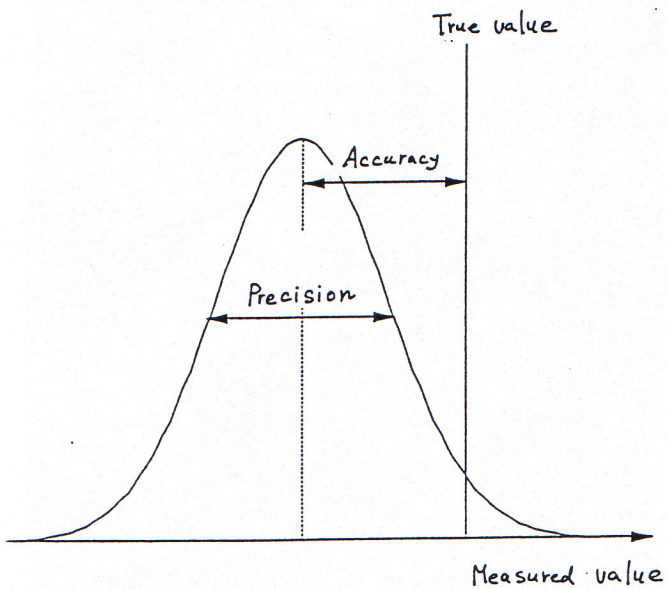
$m = 10$



$m = 20$

Three Poisson distributions: (a)  $m = 5$ , (b)  $m = 10$ , (c)  $m = 20$ .

## Accuracy & Precision



## Normal distribution

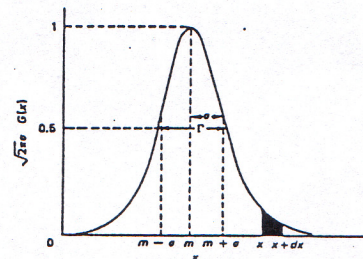
The normal distribution  $G(x)$  is given by

$$G(x) dx = \frac{1}{(\sqrt{2\pi})\sigma} \exp\left[-\frac{(x-m)^2}{2\sigma^2}\right] dx$$

where  $G(x) dx$  = probability that the value of  $x$  lies between  $x$  and  $x+dx$

$m$  = average of the distribution = 平均

$\sigma^2$  = variance of the distribution = 分散



A normal (Gaussian) distribution.

$$P(m-\sigma < x < m+\sigma) = 0.68$$

$$\Gamma = \text{半值幅} \doteq 2.35 \sigma$$

(FWHM)

### Example 3: Multiplication or Division of Counts

$$u = xy$$

$$u = \frac{x}{y}$$

$$\frac{\partial u}{\partial x} = y \text{ and } \frac{\partial u}{\partial y} = x$$

$$\frac{\partial u}{\partial x} = \frac{1}{y} \text{ and } \frac{\partial u}{\partial y} = -\frac{x}{y^2}$$

$$\sigma_u^2 = y^2 \sigma_x^2 + x^2 \sigma_y^2$$

$$\sigma_u^2 = \left(\frac{1}{y}\right)^2 \sigma_x^2 + \left(-\frac{x}{y^2}\right)^2 \sigma_y^2$$

$$\left(\frac{\sigma_u}{u}\right)^2 = \left(\frac{\sigma_x}{x}\right)^2 + \left(\frac{\sigma_y}{y}\right)^2$$

$$\left(\frac{\sigma_u}{u}\right)^2 = \left(\frac{\sigma_x}{x}\right)^2 + \left(\frac{\sigma_y}{y}\right)^2$$

### Example 4: Mean Value of Multiple Independent Counts

$$\Sigma = x_1 + x_2 + x_3 + \dots + x_N$$

$$\sigma_\Sigma^2 = \sigma_1^2 + \sigma_2^2 + \sigma_3^2 + \dots + \sigma_N^2$$

$$\sigma_{x_i} = \sqrt{x_i}$$

$$\sigma_\Sigma^2 = x_1 + x_2 + x_3 + \dots + x_N = \Sigma$$

$$\sigma_\Sigma = \sqrt{\Sigma}$$

$$\bar{x} = \frac{\Sigma}{N}$$

$$\sigma_{\bar{x}} = \frac{\sigma_\Sigma}{N} = \frac{\sqrt{\Sigma}}{N} = \frac{\sqrt{N\bar{x}}}{N}$$

$$\sigma_{\bar{x}} = \frac{\sqrt{\bar{x}}}{N}$$

### Error propagation formula

$$u = u(x_1, x_2, x_3, \dots, x_N)$$

$$\sigma_u^2 = \left(\frac{\partial u}{\partial x_1}\right)^2 \sigma_{x_1}^2 + \left(\frac{\partial u}{\partial x_2}\right)^2 \sigma_{x_2}^2 + \left(\frac{\partial u}{\partial x_3}\right)^2 \sigma_{x_3}^2 + \dots$$

### Example 1: Sums or Differences of Counts

$$u = x + y \text{ or } u = x - y$$

$$\frac{\partial u}{\partial x} = 1 \text{ and } \frac{\partial u}{\partial y} = \pm 1$$

$$\sigma_u^2 = (1)^2 \sigma_x^2 + (\pm 1)^2 \sigma_y^2 \quad \sigma_u = \sqrt{\sigma_x^2 + \sigma_y^2}$$

### Example 2: Multiplication or Division by a Constant

$$u = Ax$$

$$u = \frac{x}{B}$$

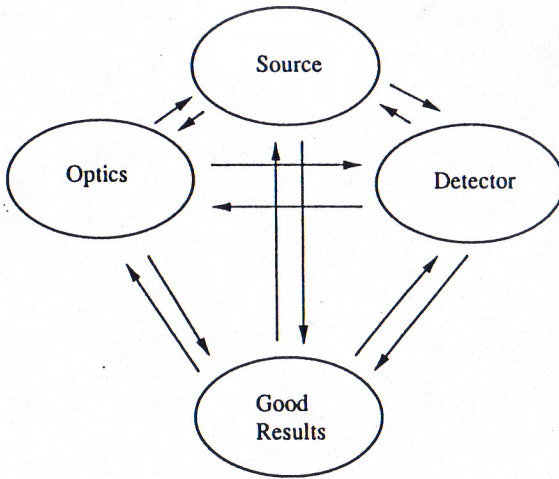
$$\frac{\partial u}{\partial x} = A$$

$$\frac{\partial u}{\partial x} = \frac{1}{B}$$

$$\sigma_u = A\sigma_x$$

$$\sigma_u = \frac{\sigma_x}{B}$$

## Trinity of X-ray Instrumentation



2

### Requirements for X-ray Detectors for Use with SR (especially for Diffraction Studies)

High counting rate (short dead time)

High sensitivity (High DQE) ----- Wide dynamic range

Linearity of response

Large active area ----- Spatial resolution

Position accuracy (small image distortion)

Uniformity of response

Ease to handle & stability

Reasonable cost ( initial & running)

Time resolution

Energy resolution

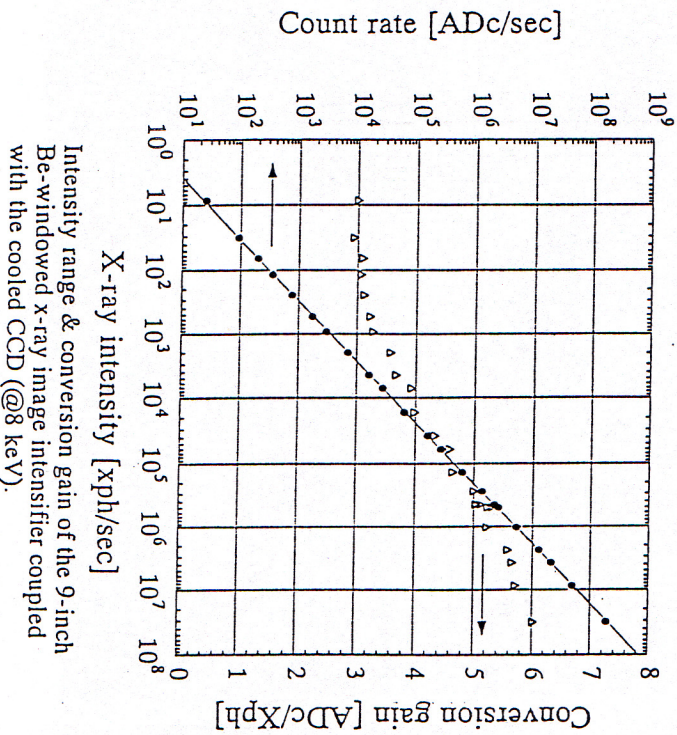
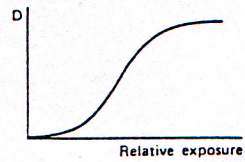
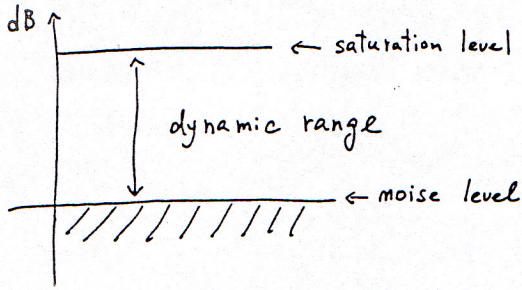
Capability for real-time measurements

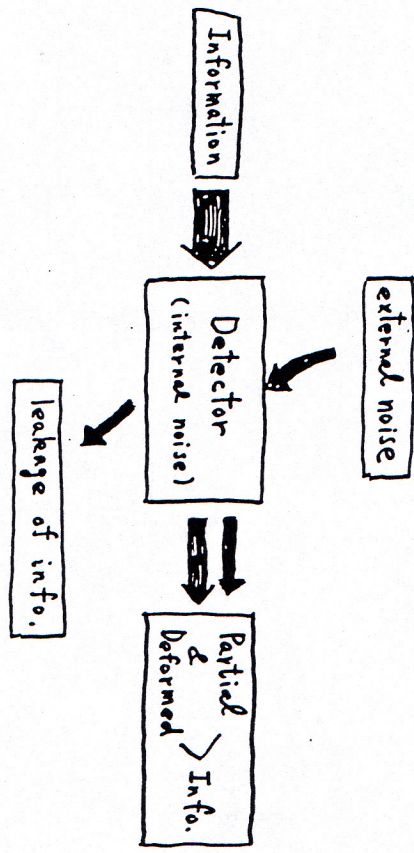
# Types of X-ray Detectors

Integration type	Ionization chamber	TLD	Photo diode array	ID-IC	Film	Imaging plate	CCD-based detector	Remarks
Pulse type	Scintillation counter	Avalanche photo diode	ID-PSPC	2D-PSPC (MW/PC)	SSD(Si, Ge)	Hg12, CdTe	Bolometer	High sensitivity Good linearity Wide D-range
Point	One dimensional I(x)	Two dimensional I(x,y)	Energy dimensional I(E)	Remarks				

$$\text{dynamic range} = 20 \cdot \log \frac{\text{saturation level}}{\text{noise level}} \text{ [dB]}$$

$$= 10 \cdot \log \frac{[\text{sat. level}]^2}{[\text{noise level}]^2} \text{ [dB]}$$





## Efficiency of detectors

### Definition I

$$RQE = \frac{\text{number of output events}}{\text{number of input events}}$$

Responsive Quantum Efficiency

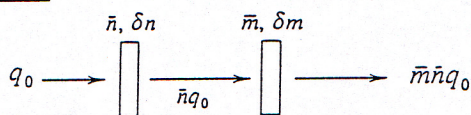
### Definition II

$$DQE = \frac{\left(\frac{S}{N}\right)_{\text{output}}^2}{\left(\frac{S}{N}\right)_{\text{input}}^2}$$

Detective Quantum Efficiency

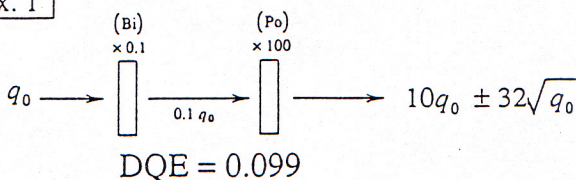
## Propagation of Errors

### Theory

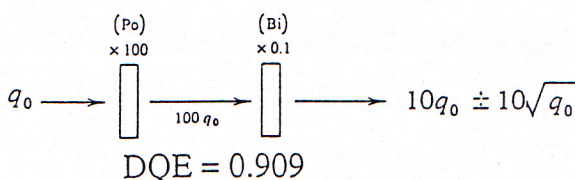


$$DQE = \frac{1}{1 + \left(\frac{\delta n}{\bar{n}}\right)^2 + \frac{1}{\bar{n}} \left(\frac{\delta m}{\bar{m}}\right)^2}$$

### ex. 1

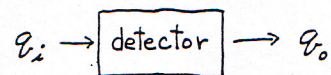


### ex. 2



incident

detected (or counted)

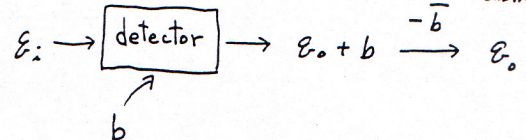


$$DQE = \frac{\left(\frac{S}{N}\right)_{\text{out}}^2}{\left(\frac{S}{N}\right)_{\text{in}}^2} = \frac{\left(\frac{E_o}{\sqrt{E_o}}\right)^2}{\left(\frac{E_i}{\sqrt{E_i}}\right)^2} = \frac{E_o}{E_i}$$

incident

detected

B.G. subtracts



$$DQE = \frac{\left(\frac{E_o}{\sqrt{E_o + 2b}}\right)^2}{\left(\frac{E_i}{\sqrt{E_i}}\right)^2} = \frac{E_o^2}{E_i(E_o + 2b)} = \frac{E_o}{E_i} \cdot \frac{1}{\left(1 + \frac{2b}{E_o}\right)}$$

in case of  $E_o \sim b$

$$DQE \approx \frac{E_o}{E_i} \cdot \frac{1}{1 + 2} = \frac{1}{3} \cdot \frac{E_o}{E_i}$$



# Spatial resolution

PSF: Point Spread Function  
LSF: Line Spread Function

MTF: Modulation Transfer Function

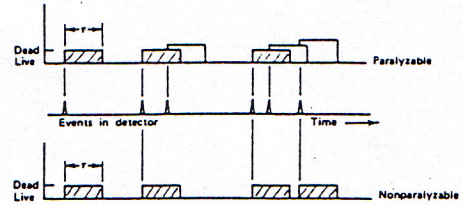
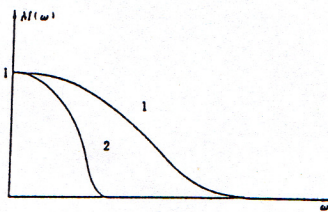
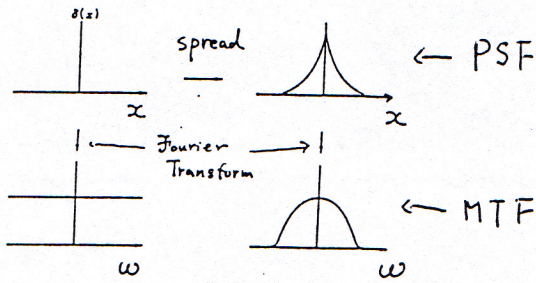


Figure 4-7 Illustration of two assumed models of dead time behavior for radiation detectors.

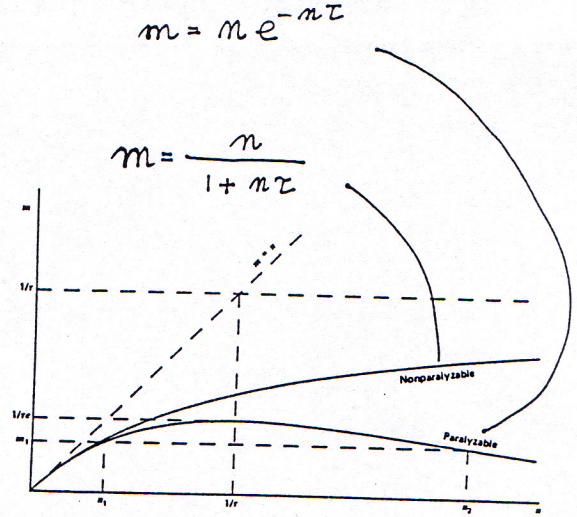
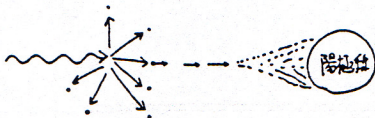


Figure 4-8 Variation of the observed rate  $m$  as a function of the true rate  $n$  for two models of dead time losses.

# Energy Resolution



$$m_0 \cdot A = \frac{E_{photon}}{W} \times A$$

$$Q = m_0 e \cdot \bar{A}$$

$$\left(\frac{\sigma(Q)}{Q}\right)^2 = \left(\frac{\sigma(m_0)}{m_0}\right)^2 + \frac{1}{m_0} \cdot \left(\frac{\sigma(A)}{A}\right)^2 \quad (8)$$

$$\left(\frac{\sigma(m_0)}{m_0}\right)^2 = \frac{F}{m_0} \quad F: 0.05 \sim 0.2$$

Fano Factor.

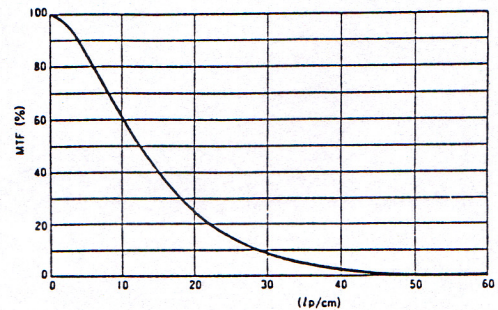
W

- SSD  $\sim 3 \text{ eV} / e^- \text{-hole}$
- Gas Proportional Counter  $\sim 30 \text{ eV} / e^- \text{-ion}$
- Emulsion  $\sim 3 \text{ keV} / \text{grain}$

35 (lp/cm) at MTF 5%



• MTF:



# TLD (Thermoluminescent Dosimeter)

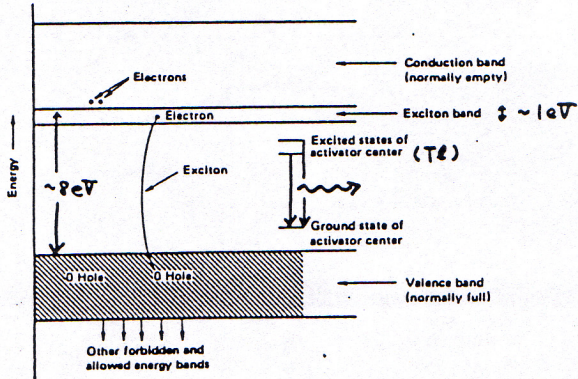
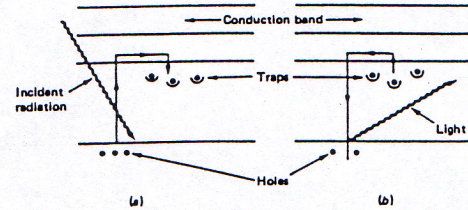
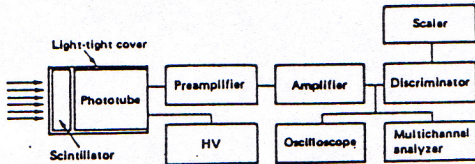


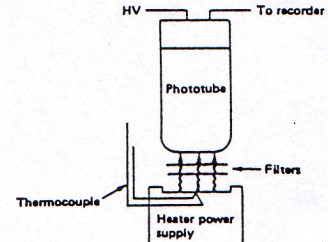
FIG. 6.2 Allowed and forbidden energy bands of a crystal.



(a) As a result of irradiation, some carriers fall into traps. (b) Upon heating, the carriers are given enough energy to escape from the traps and return to the valence band, with the emission of light.



A detection system using a scintillator.



A set-up used to read a TLD.

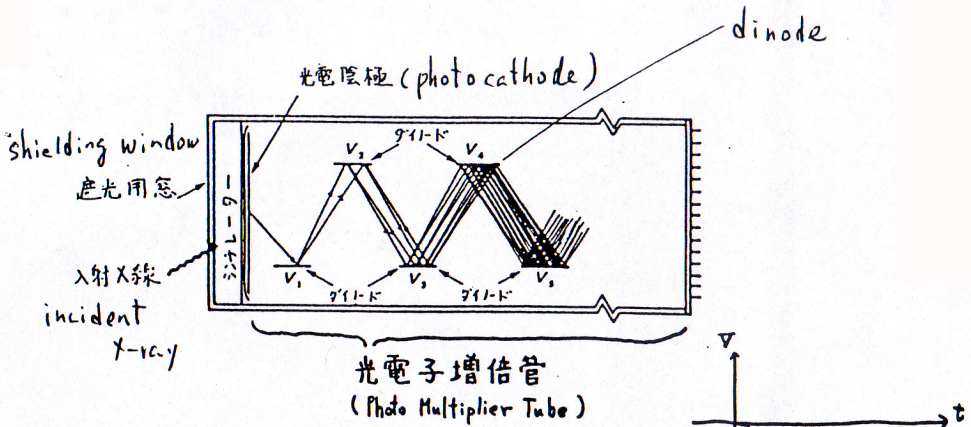
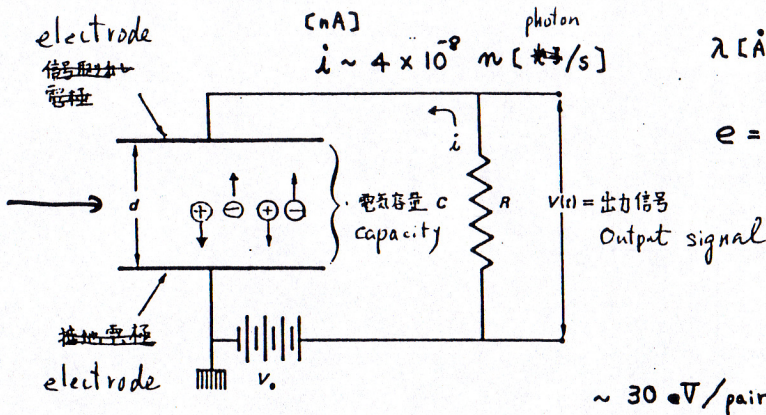


図4 シンチレーションカウンターの構造

Structure of Scintillation Counter

17.100 X線エネルギー  
X-ray Energy



$$\lambda [\text{\AA}] = \frac{12.4}{E [\text{keV}]}$$

$$e = 1.6 \times 10^{-19} \text{ [C]}$$

$$\sim 30 \text{ eV/pair}$$

for 9 keV X-ray ( $\lambda = 1.4 \text{ \AA}$ )

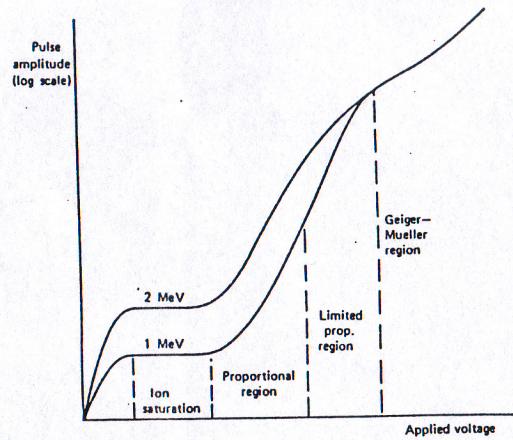
$$\frac{9000 \text{ [eV]}}{\sim 30 \text{ [eV]}} = 300 \text{ e-ion pair}$$

Structure of Ionization chamber

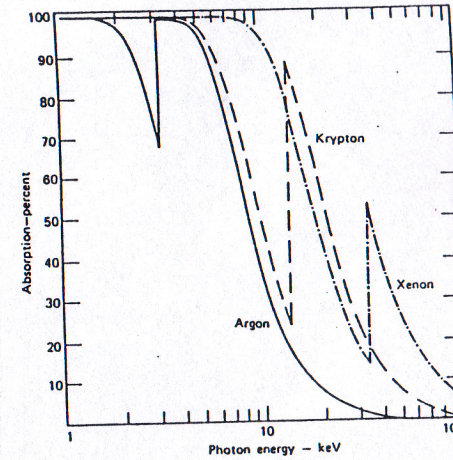
図2 電離箱の動作原理

~~電流を電圧に変換する。~~

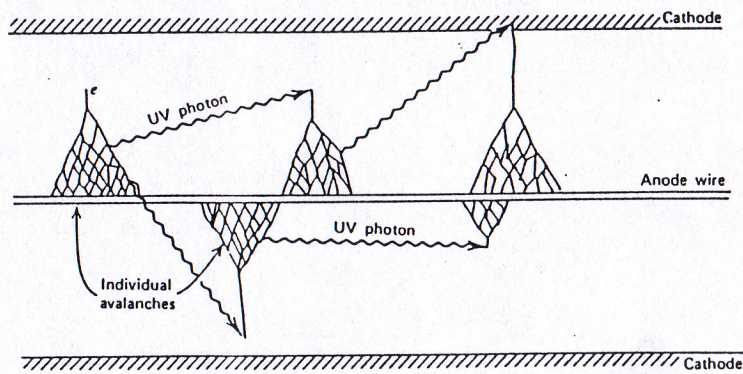
Electric current is converted to voltage.



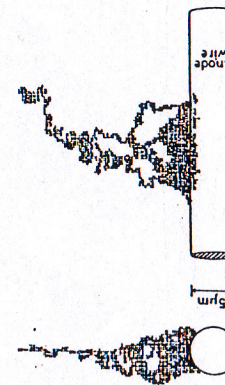
**Figure 6-2** The different regions of operation of gas-filled detectors. The observed pulse amplitude is plotted for events depositing two different amounts of energy within the gas.



**Figure 6-14** Fraction of incident photons absorbed in a 5.08 cm thick layer of several proportional gases at 1 atm pressure.

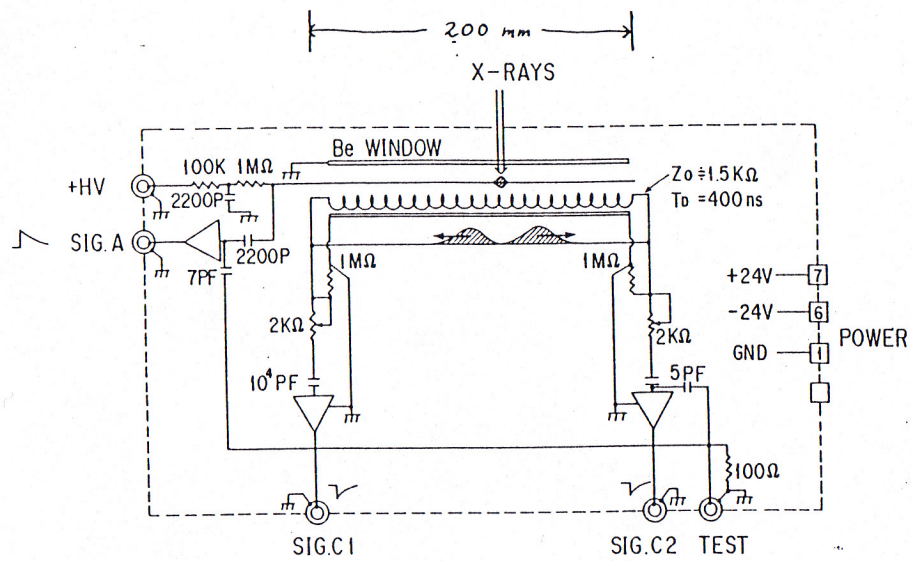


**Figure 7-1** The mechanism by which additional avalanches are triggered in a Geiger discharge.



**Figure 6-4** Orthogonal views of an avalanche triggered by a single electron as simulated by a Monte Carlo calculation. The density of the shading indicates the concentration of electrons formed in the avalanche. (From Matoba et al.)

Space charge limits the count rate!  
(空間電荷)



Schematic diagram of electronics of the linear PSD

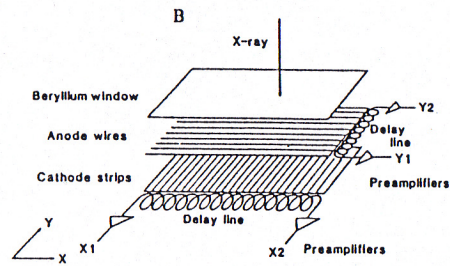
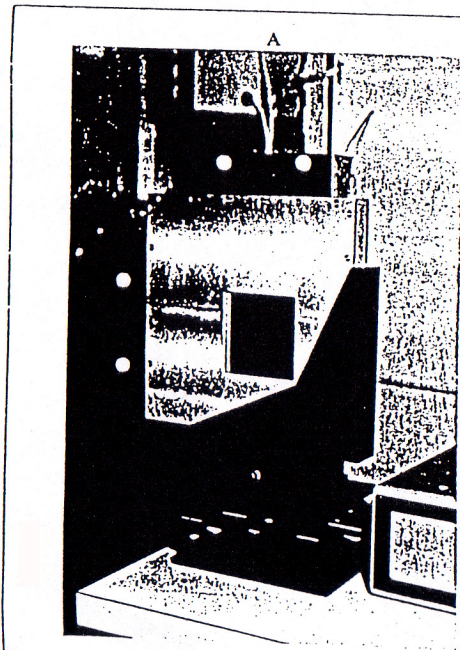
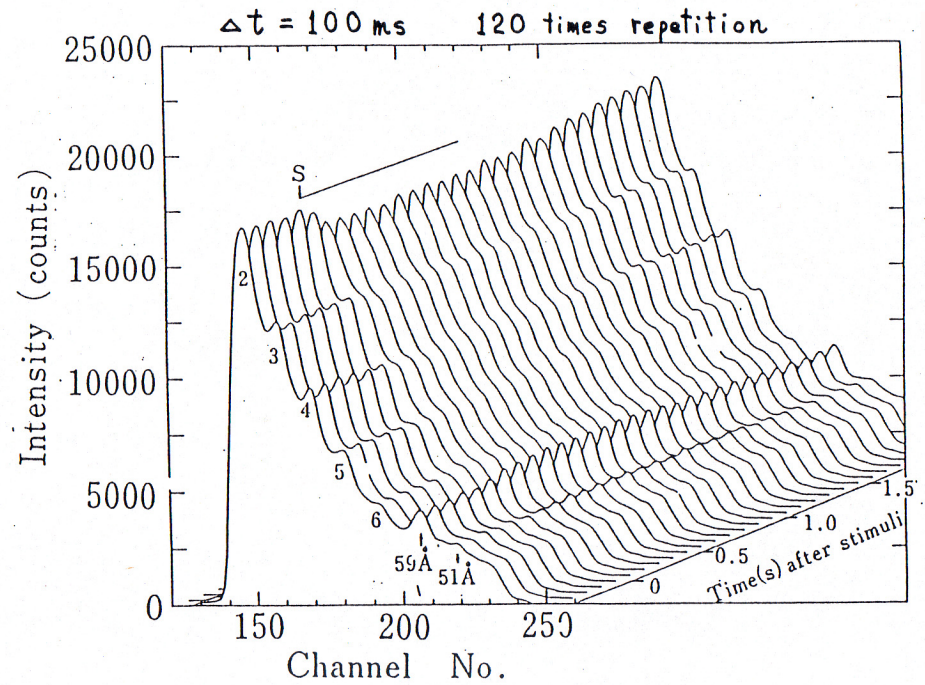
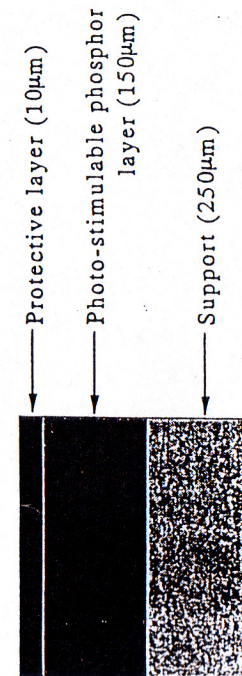


Fig. 1 Structure of the multi-wire chamber.  
 A: Front view of the two-dimensional detector.  
 B: The chamber consisted of a beryllium window, an anode and a cathode planes with a spacing 5 mm. The anode plane was made of gold-plated tungsten wires 10  $\mu\text{m}$  in diameter, 2 mm apart, while cathode plane was made of the copper strips, 2 mm apart, orthogonal to the anode wires. The chamber was filled with a gas mixture of 90% argon and 10% methane at a pressure of 1 atm.



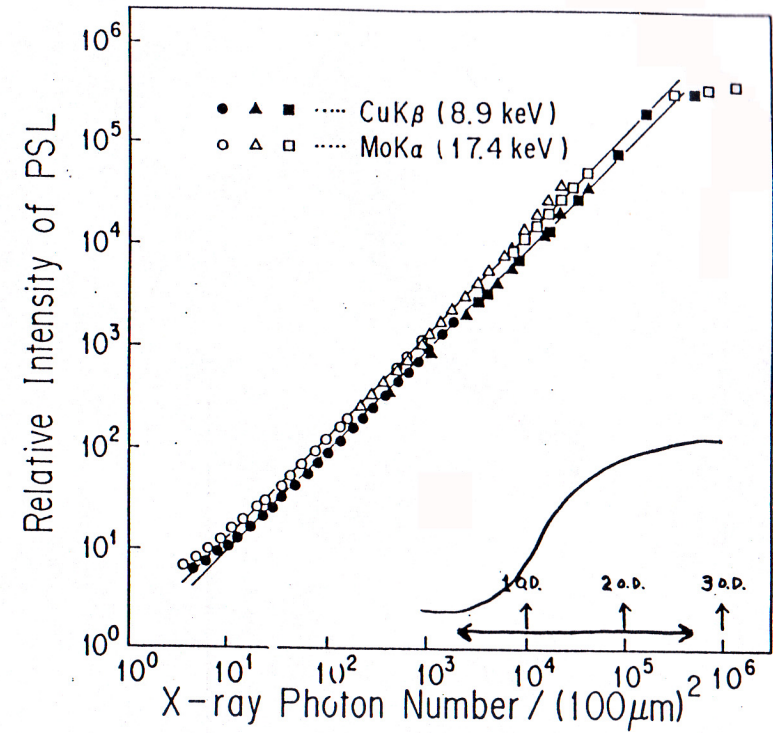
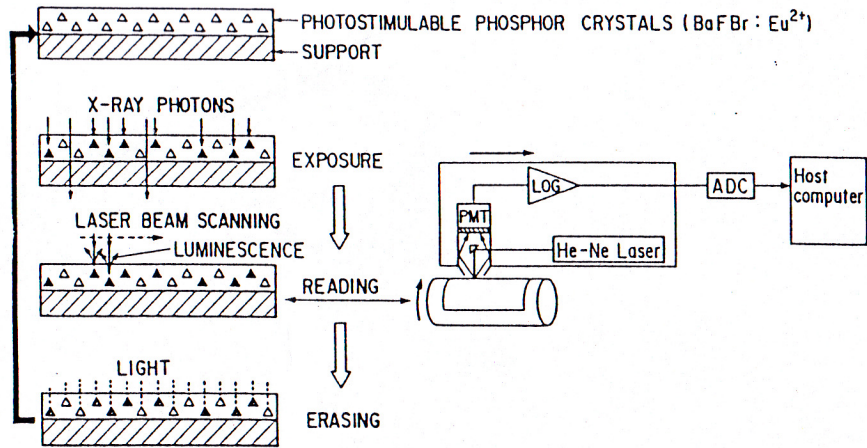
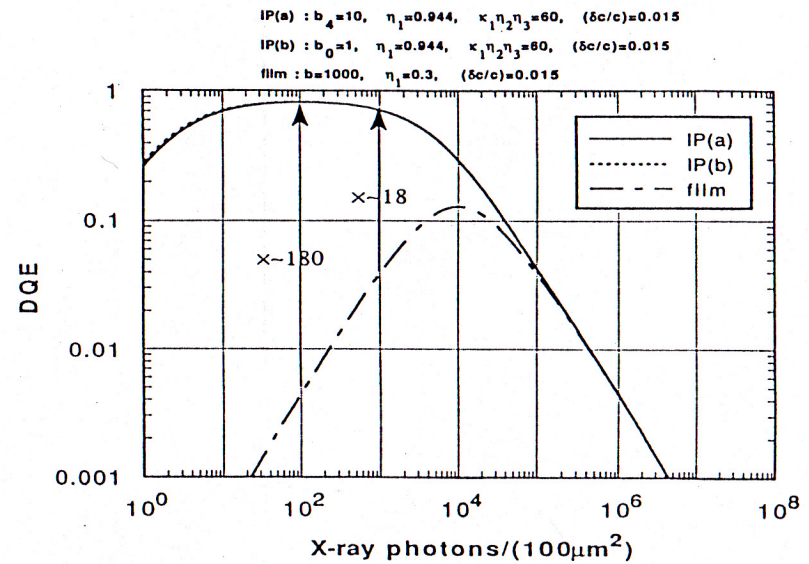
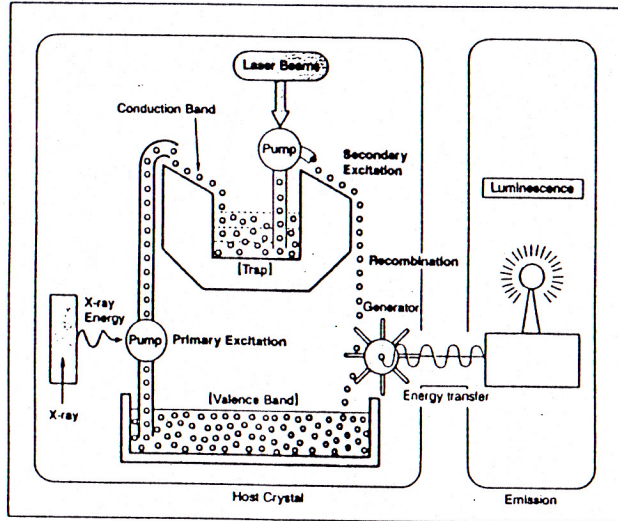
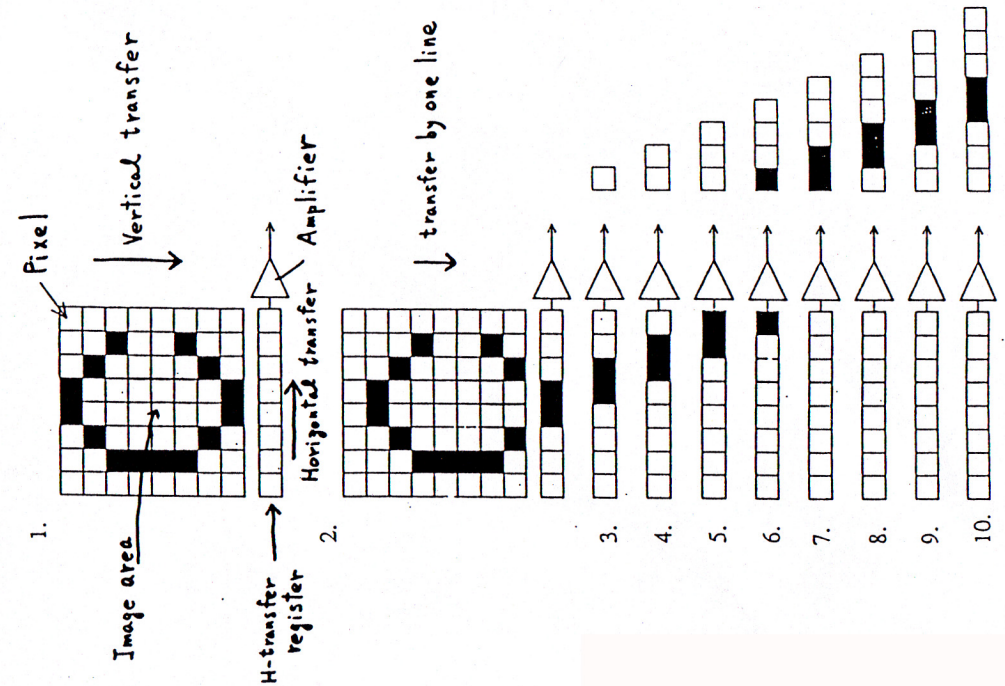
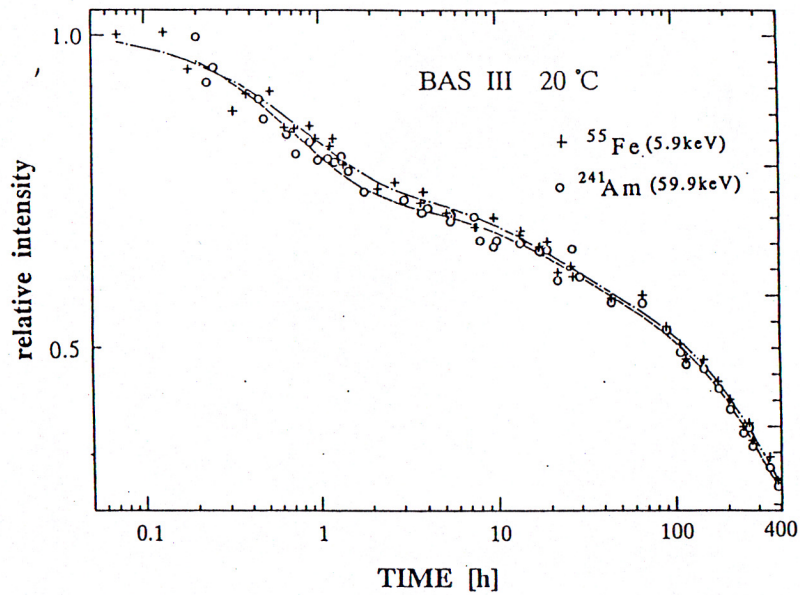


Photo-stimulated Luminescence Mechanisms



検出量子効率 (DQE) の入射 X 線量依存性



### Application field of the Imaging Plates

Protein crystallography  
Weissenberg camera  
Oscillation camera  
Laue method

Laue diffraction of micro-crystal

Small-angle x-ray scattering

X-ray diffraction under high pressure

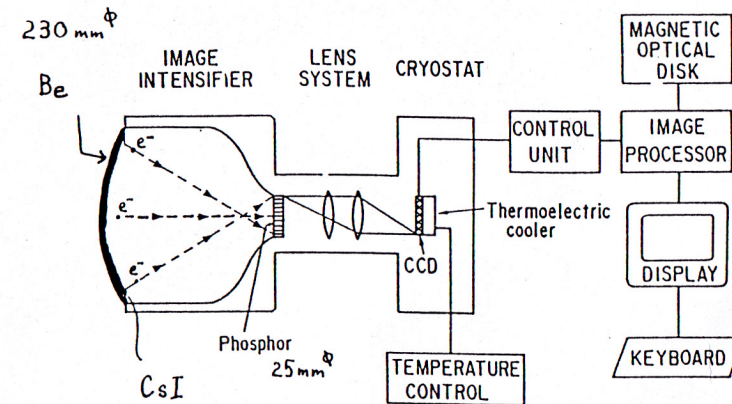
X-ray diffuse scattering

Compton X-ray scattering spectroscopy

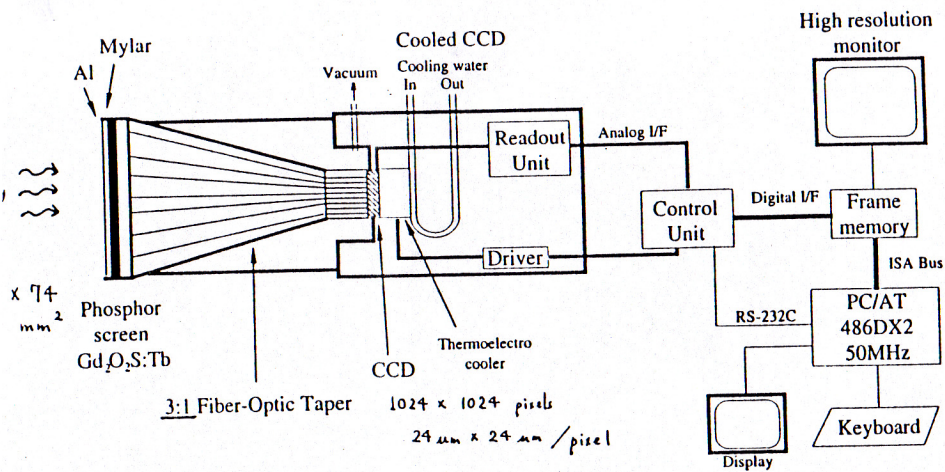
Dispersive XAFS

X-ray topography

Angiography



Schematics of the X-ray TV detector which utilizes the Be-window X ray image intensifier together with a cooled or a TV-rate CCD.



Schematics of a Fiber-coupled CCD detector

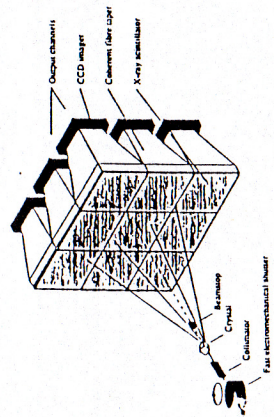


Figure 4 Example of a typical 3 x 3 mosaic CCD detector. The full active aperture of this system is approximately 150 x 150 mm. All the CCDs can be read out in parallel, with typically four output channels per device. Adapted from Westbrook (1988).

### Comparison of three x-ray area detectors

	Advantage	Application	Drawback
IP	Good uniformity Large area size	static precise measurement slow time-resolved measurement	Long readout time 1 ~ 2 min. off-line
II+CCD	High DQE Short readout time 1 ~ 4 ε	time-resolved measurement	Image distortion of II (variant) delicate, complex
FOT+CCD	Stability Short readout time 1 ~ 4 ε	automated static measurement ↓ protein crystallography	Limited area size Image distortion of FOT (invariant)

Signal/xph  
r.m.s. noise

IP

1 ~ 3

XII ⊕ CCD

5 ~ 10

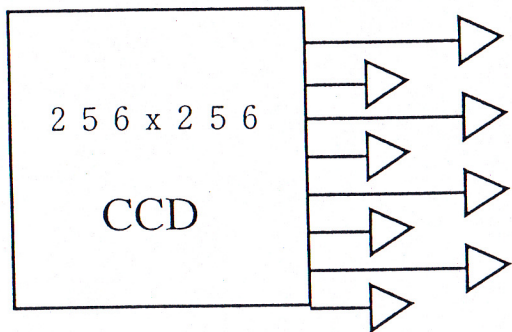
FOT ⊕ CCD

0.3 ~ 1

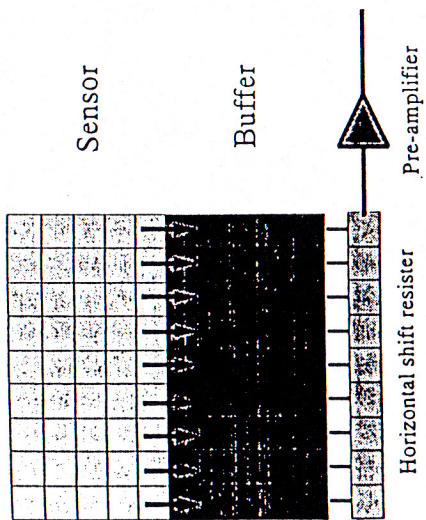
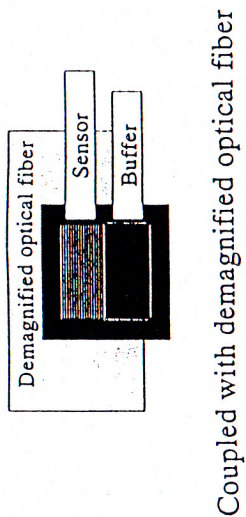


CCD with multi-channel readout  
 CCDの多チャンネル読み出し

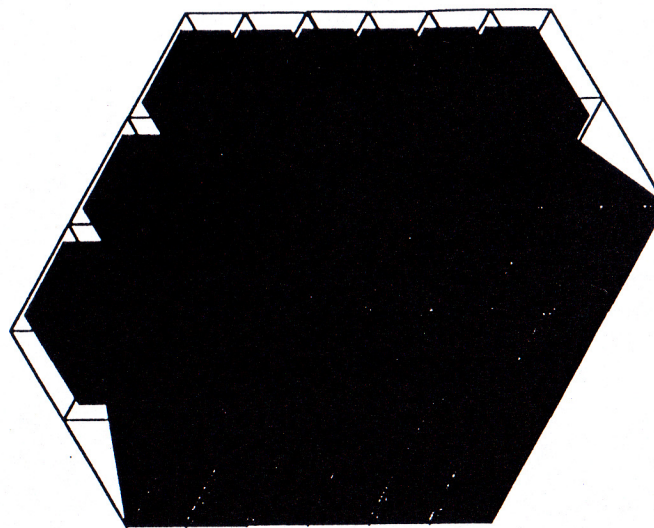
8チャンネル → 1000 frame/s (1ms)



4x4 スーパーピクセル読み出し → 8000 frames/s (125 μs)  
 Super-pixel readout

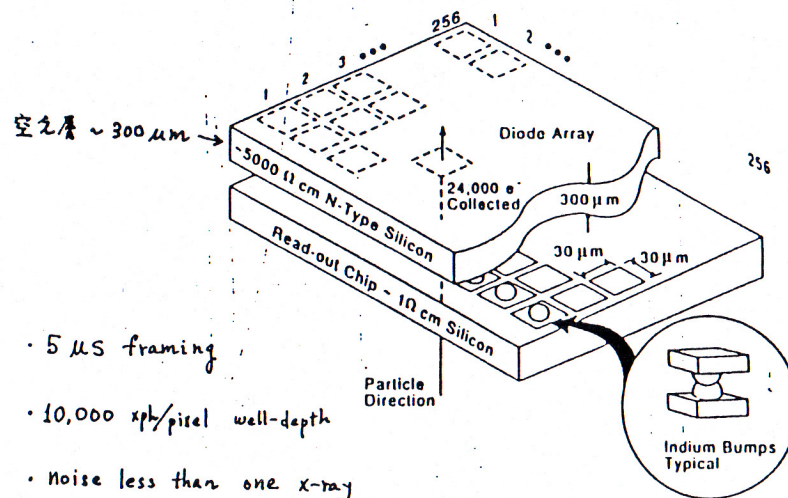


Buffered frame transfer-type CCD



Schematics of the arrayed CCD  
 x-ray detector  
 (in the case of 3 x 6 system).

PAD



- 5 μs framing
- 10,000 xph/pixel well-depth
- noise less than one x-ray

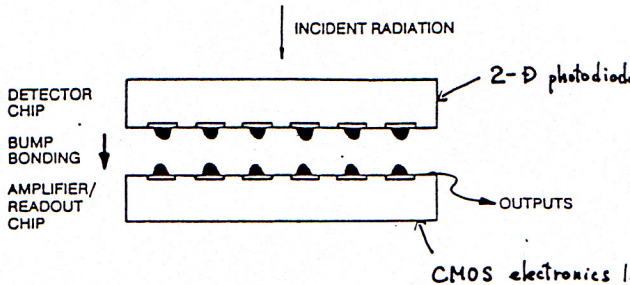
# PAD : Pixel Arrayed Detector

## Basic Configuration

Separate Sensor + Readout Chips

Joined by 2-Dimensional Array

of Indium Bump Bonds



pixel :  $150 \mu\text{m} \times 150 \mu\text{m}$

No. of pixel :  $1024 \times 1024$