

JASS'02

A-Salt, Jordan, October 2002

The structure of liquid surfaces

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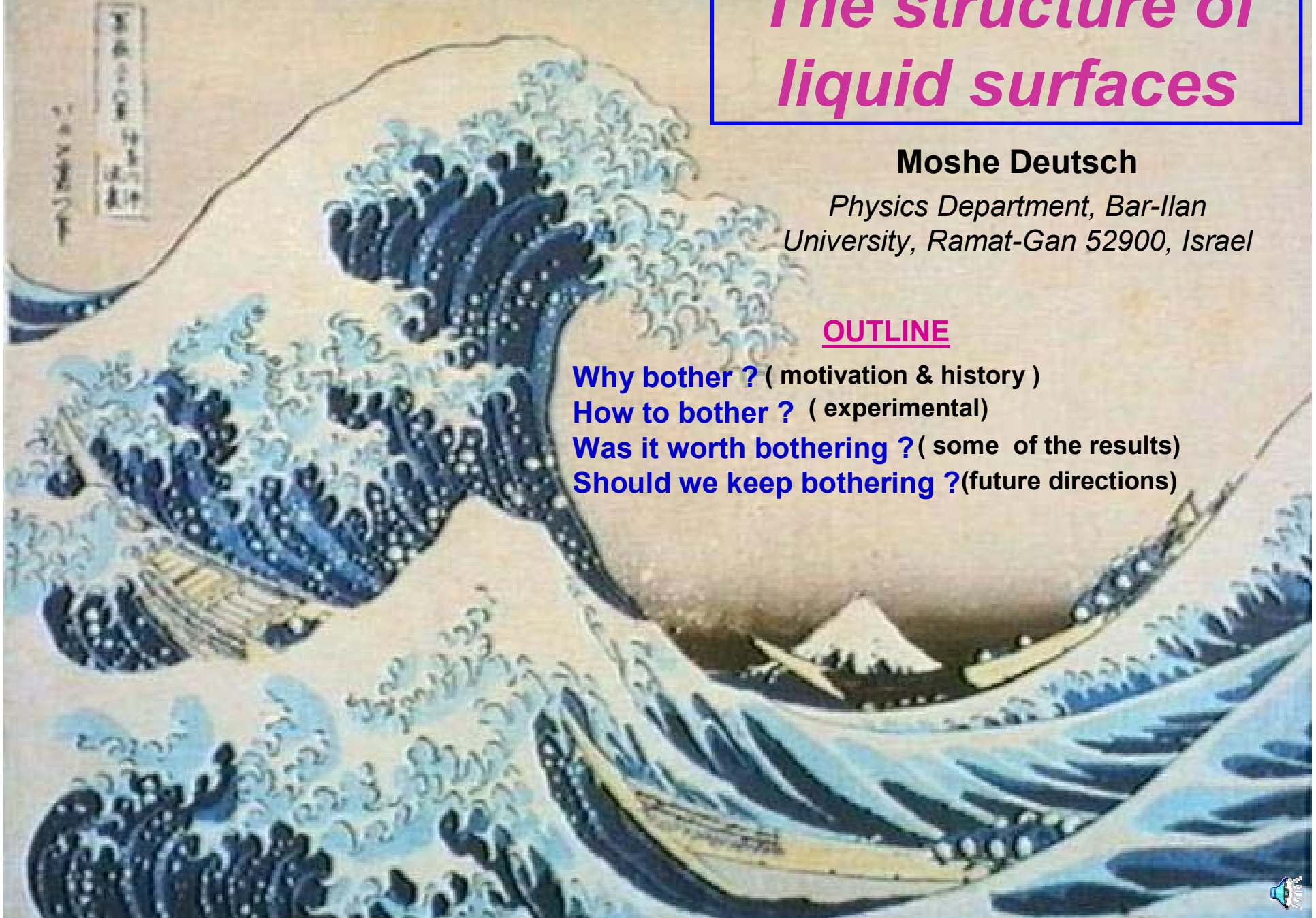
OUTLINE

Why bother ? (motivation & history)

How to bother ? (experimental)

Was it worth bothering ? (some of the results)

Should we keep bothering ? (future directions)



Motivation & History

On the one hand:

- Bulk liquids are boring: no order, no defects, no phases/transitions...
- Theory very difficult: No comprehensive theory to date.

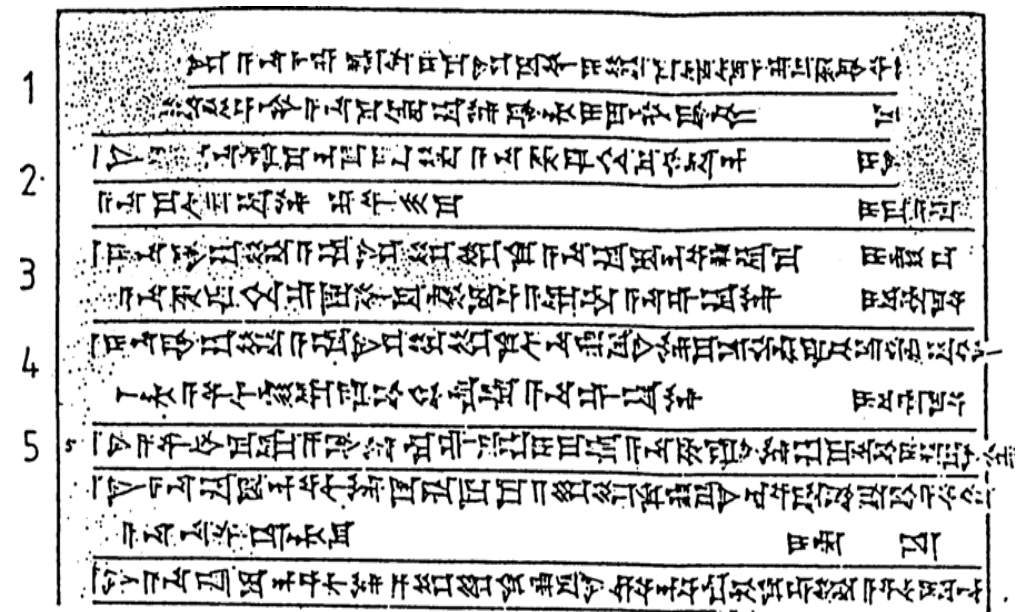


∴ The surface of a boring bulk must be a boring surface :

On the other hand:

- Liquid surfaces have attracted interest (not always scientific) since ancient times. (Bible, China, Greece, Ben Franklin)
- X-ray methods developed only in 1982-6.
- Increasing number of studies since then.

Atomic resolution liquid surface studies reveal many new and intriguing effects !

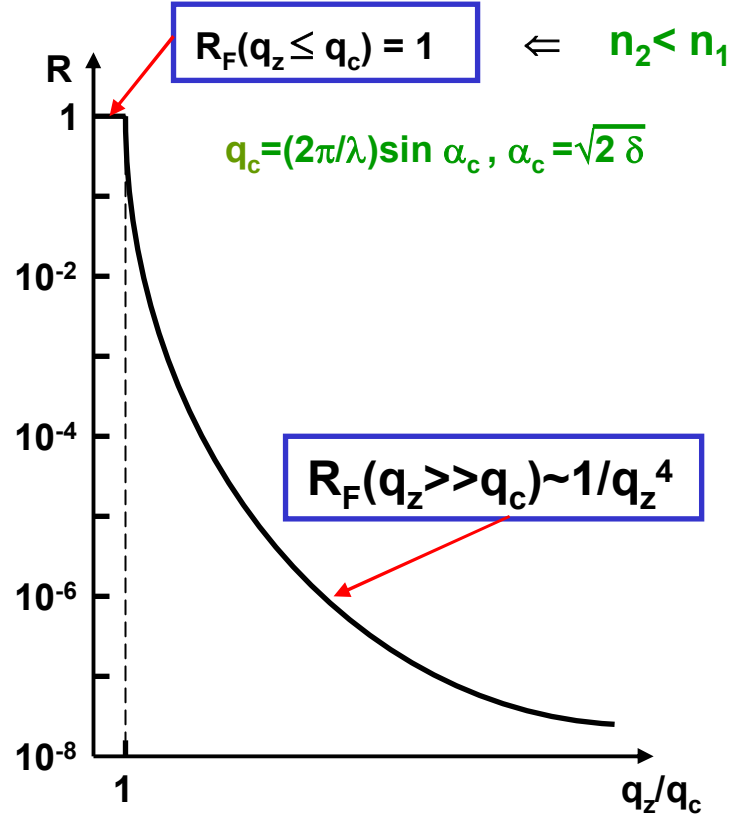
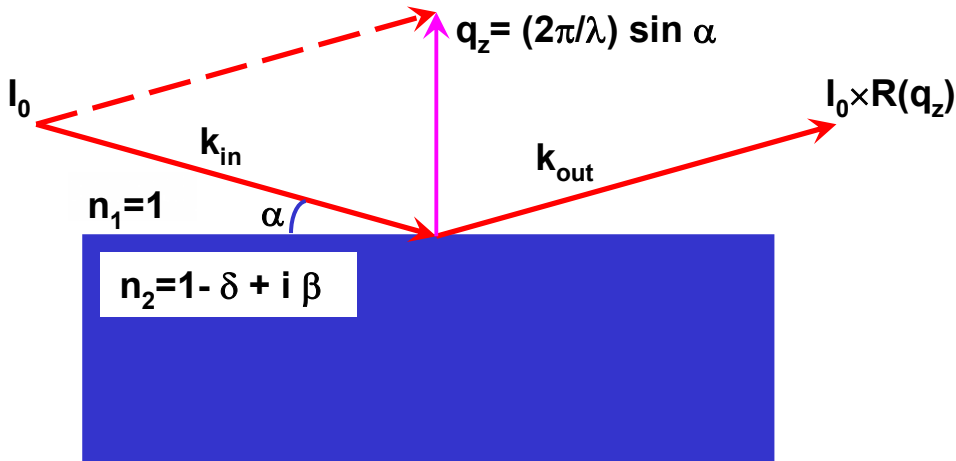


The art of lecanomancy (Hamurabi, 18th century B.C.E.)
 The spreading of oil on water in a ceremonial bowl

- (1) Oil sinks, rises and spreads: war-lost sick- divine punishment
- (2) Oil splits in two: war-both camps march together sick- death
- (3) Single oil drop emerges in the east: war-booty sick-recovery
- (4) 2 drops (large & small): male child will be born sick- recovery
- (5) Oil fills bowl: war-defeat for the leader sick- death

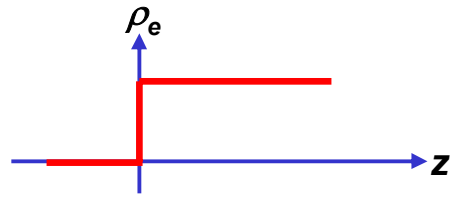


X-Ray Reflectivity (I)



For a surface which is:

- (1) flat
- (2) abrupt



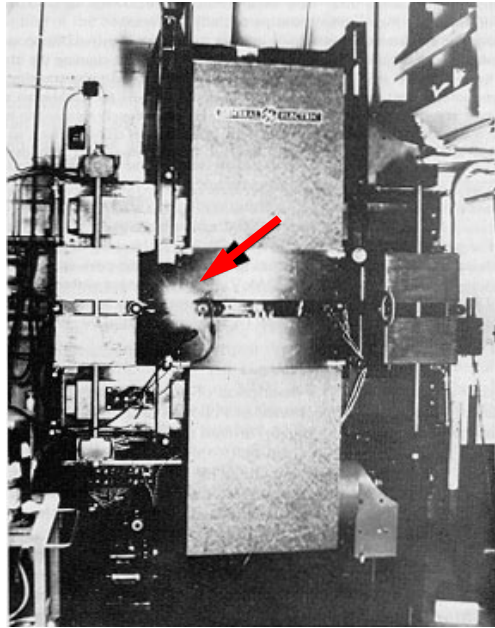
Fresnel reflectivity

$$R_F(q_z) = \left| \frac{q_z - \sqrt{q_z^2 + q_c^2}}{q_z + \sqrt{q_z^2 + q_c^2}} \right|^2$$

- High resolution \Leftrightarrow high q_z .
- $q_z/q_c \approx 50 \Rightarrow R = 10^{-8}$, (for $H_2O \Rightarrow Res. \sim 6 \text{ \AA}$ only).
- High intensity source required \Rightarrow **Synchrotron !**



Synchrotron !!



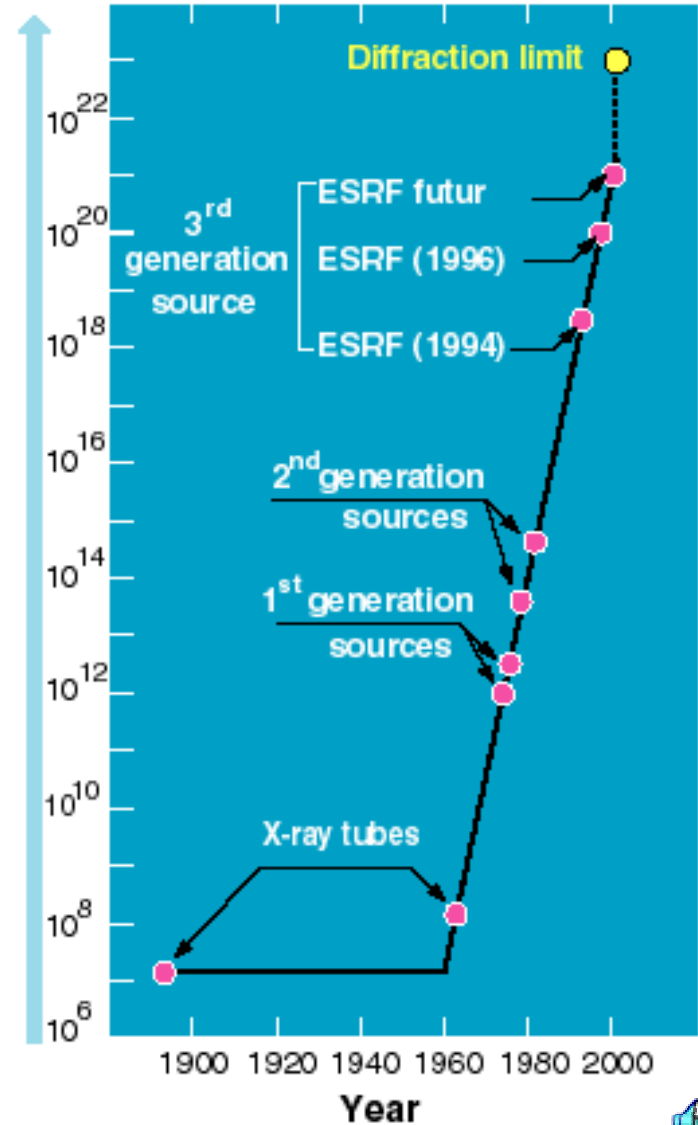
The GE 70 MeV synchrotron, 1947

Evolution of x-ray intensity

The ESRF 6GeV Synchrotron, 1994



Brilliance of the X-ray beams
(photons / s / mm² / mrad² / 0.1% BW)

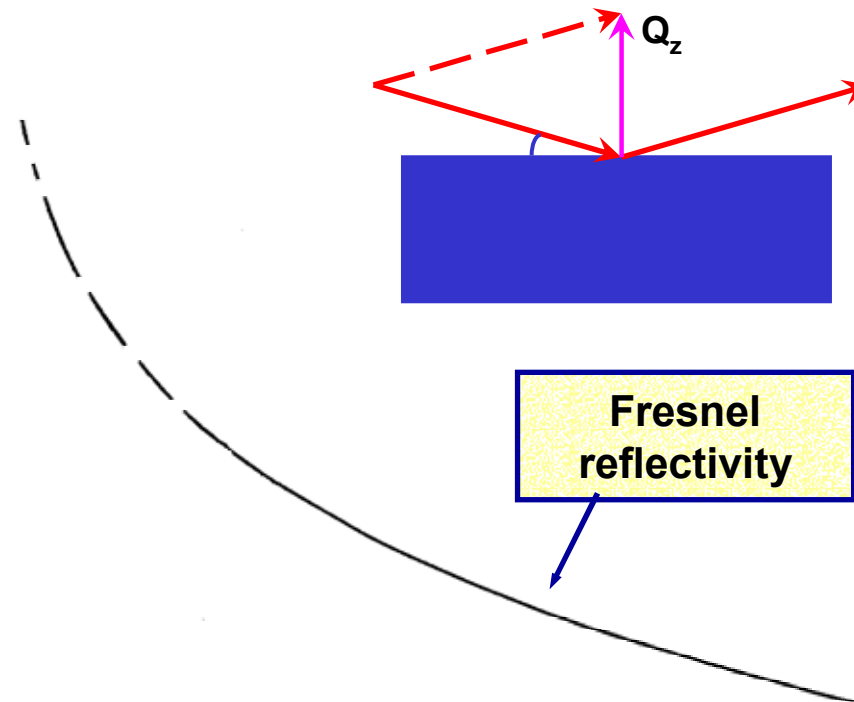


The surface of liquid water (I)

- Looks like pure Fresnel
- Surface must be abrupt and flat.

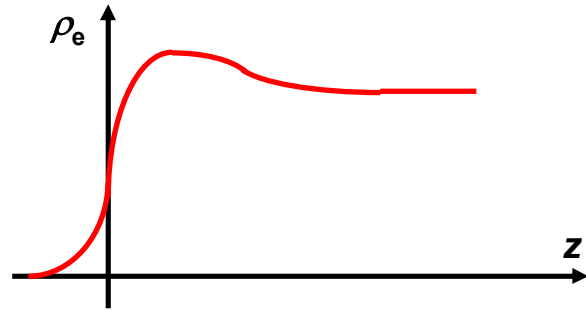
However →

- Why the deviation ?
- How to analyze non-Fresnel reflectivities



X-Ray Reflectivity (II)

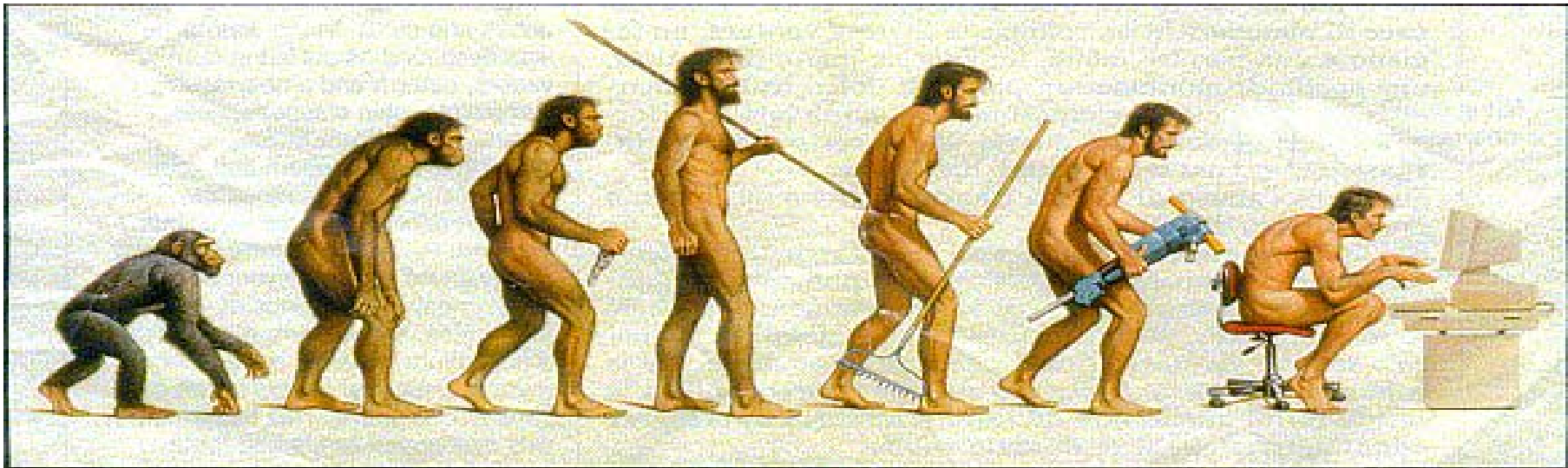
Arbitrary density profile:



$$\frac{R(q_z)}{R_F(q_z)} = \frac{1}{\rho_\infty^2} \left| \int_{-\infty}^{+\infty} \frac{d\langle \rho_e(z) \rangle}{dz} \exp(iq_z z) dz \right|^2$$

THUS...

- (1) Measure $R(q_z)$.
- (2) Divide by $R_F \Rightarrow$ measured $R(q_z)/R_F(q_z)$.
- (3) Construct model for $\rho_e(z)$.
- (4) Calculate $|\dots|^2$ for model.
- (5) Fit calculated $|\dots|^2$ to measured $R(q_z)/R_F(q_z) \Rightarrow$ **model parameters**.

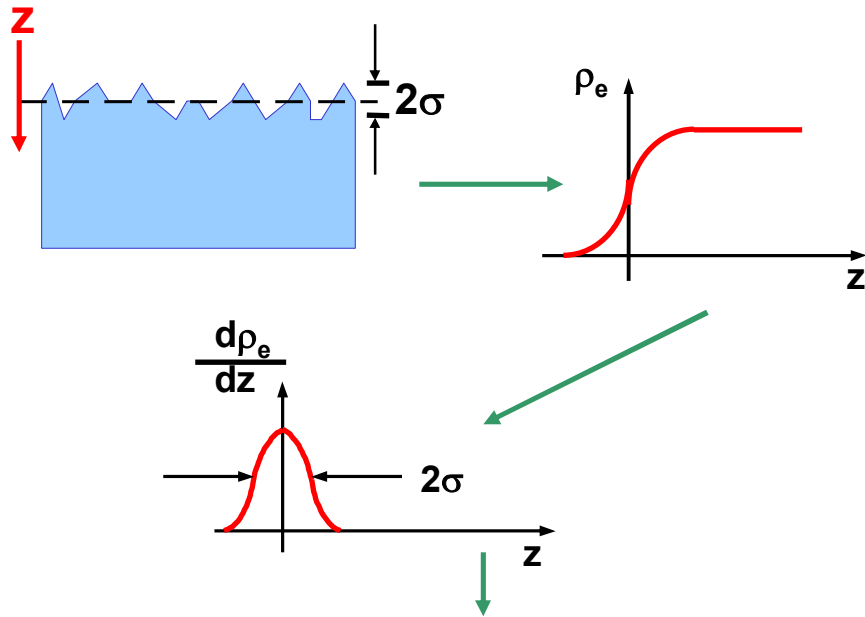


Somewhere, something went terribly wrong



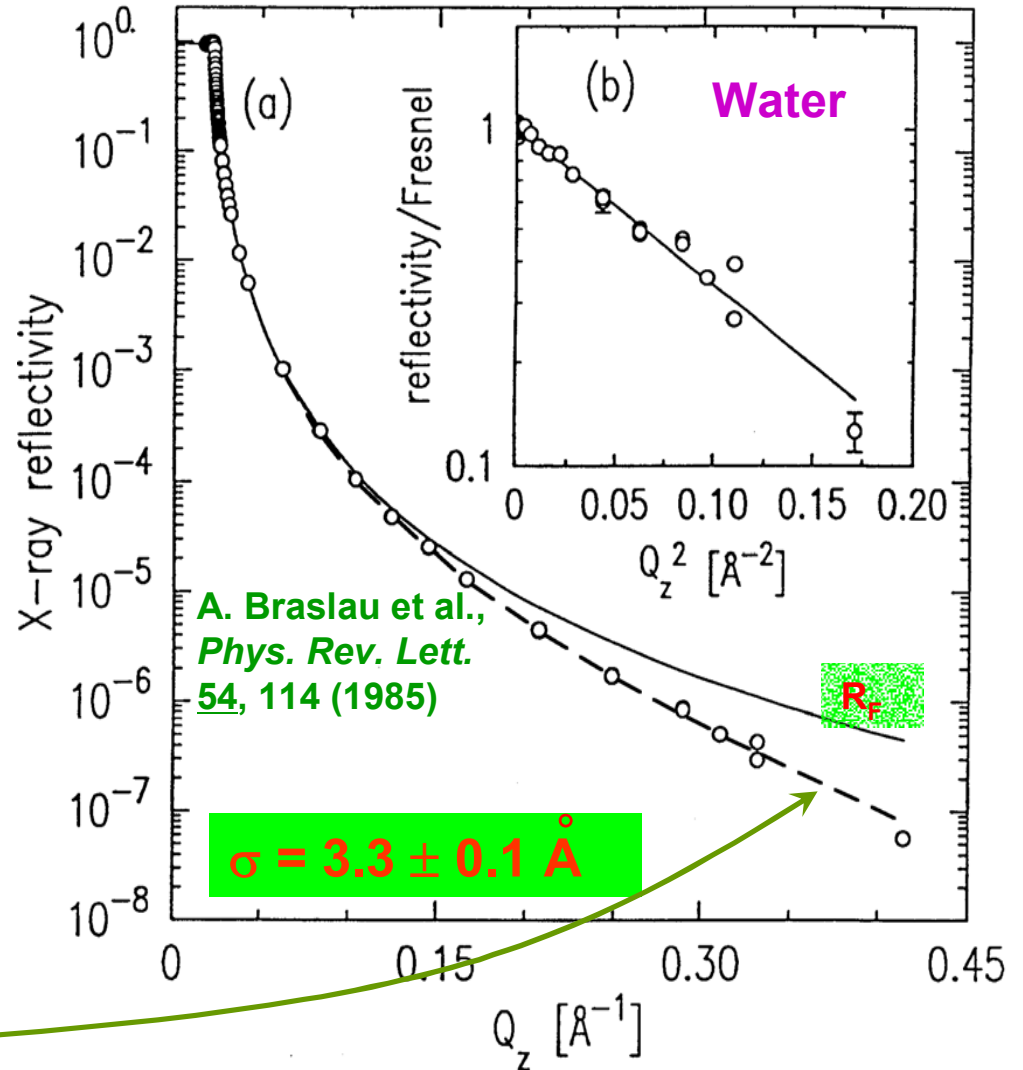
X-Ray Reflectivity (III)

Example: Gaussian surface roughness



$$\frac{R(q_z)}{R_F(q_z)} = \frac{1}{\rho_\infty^2} \left| \int_{-\infty}^{+\infty} \frac{d\langle \rho_e(z) \rangle}{dz} \exp(iq_z z) dz \right|^2$$

$$\frac{R(q_z)}{R_F(q_z)} = \exp(-q_z^2 \sigma^2)$$



A. Braslau et al.,
Phys. Rev. Lett.
 54, 114 (1985)

Where does the roughness come from ?



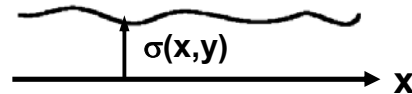
Capillary waves (I)

Where does the roughness come from ?

A. Braslau et al., *Phys. Rev. Lett.* **54**, 114 (1985)

Thermally excited capillary waves are common to all liquid surfaces.

Start with:



Equipartition of surface energy and averaging over all modes yields:

$$\langle \sigma^2 \rangle = \frac{k_B T}{2\pi} \int_{q_{\min}}^{q_{\max}} \frac{q dq}{\Delta \rho g + \gamma q^2}$$

Cutoffs are determined by the atomic size (q_{\max}) and resolution or gravitation (q_{\min}).

Taking into account non-capillary contributions:

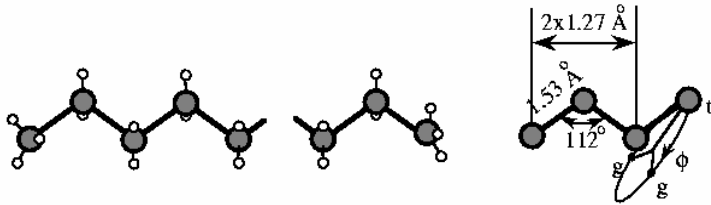
$$\sigma^2 = \sigma_0^2 + \sigma_{\text{cw}}^2 = \sigma_0^2 + \frac{k_B T}{4\pi\gamma} \ln\left(\frac{q_{\max}^2}{q_{\min}^2}\right)$$

Using this for water yields $\sigma = 3.2 \text{ \AA} !$



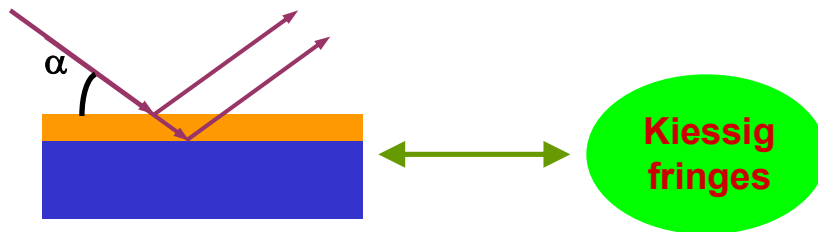
Molten chain molecules

Alkanes (C_n): $CH_3-(CH_2)_{n-2}-CH_3$:
planar, zig-zag, chain molecule.



- Basic building block of organic molecules
- Determines the molecules' properties
- Of great scientific and commercial interest

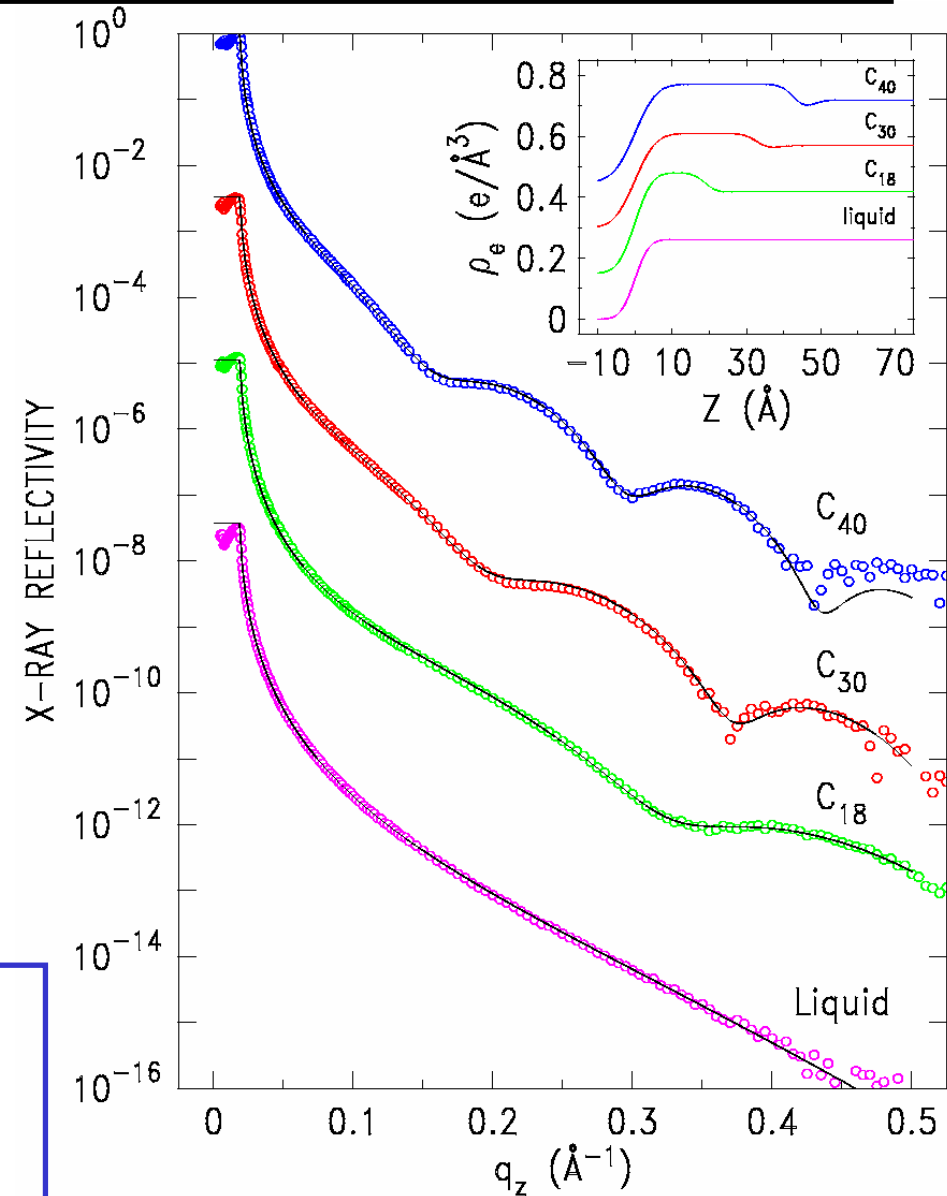
What is the structure of the melt's surface ?
 How does it change with temperature ?



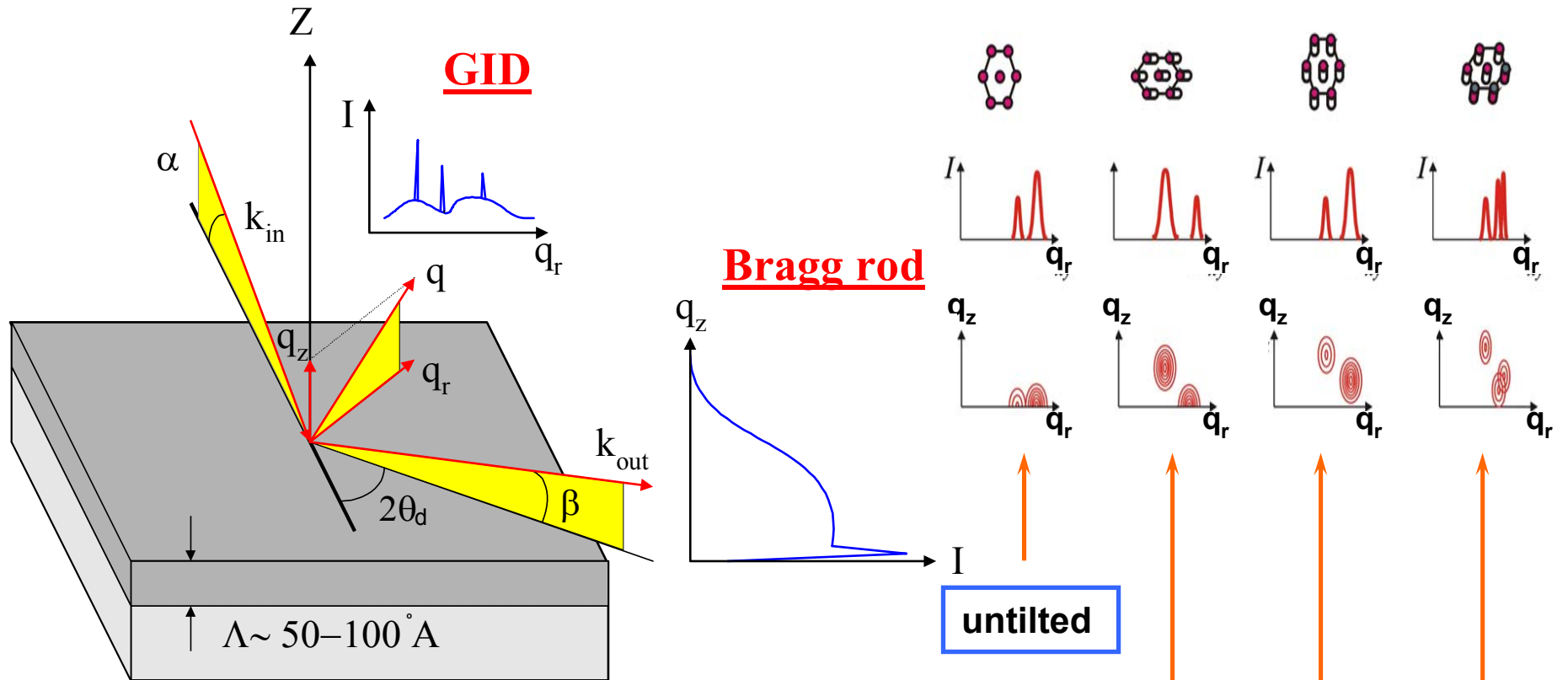
Surface Layer

- Appears at T_s close to, but above T_f .
- A single dense monolayer is formed.

Is it a solid ?



X-ray in plane scattering geometry



- Incidence at $\alpha < \alpha_c \Rightarrow$ low penetration, $\sim 50 \text{ \AA}$, \Rightarrow small bulk contribution.
- GID depends on $q_r \Rightarrow$ probes in-plane order.
- BR depends on q_z at q_r peaks \Rightarrow probes molecular tilt.

untitled

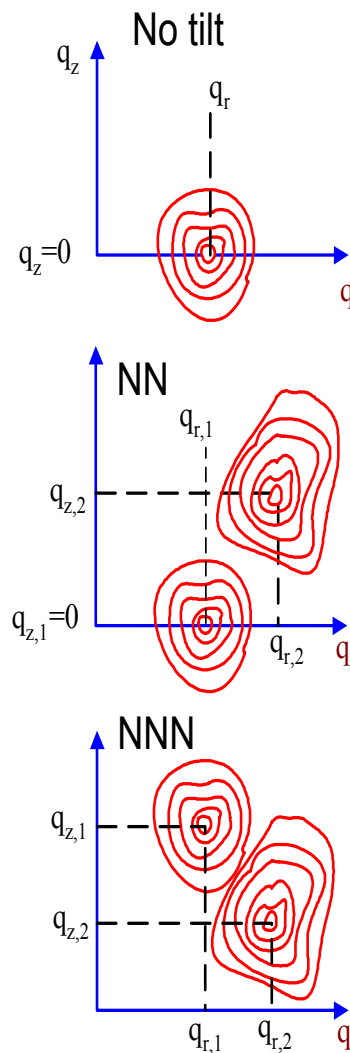
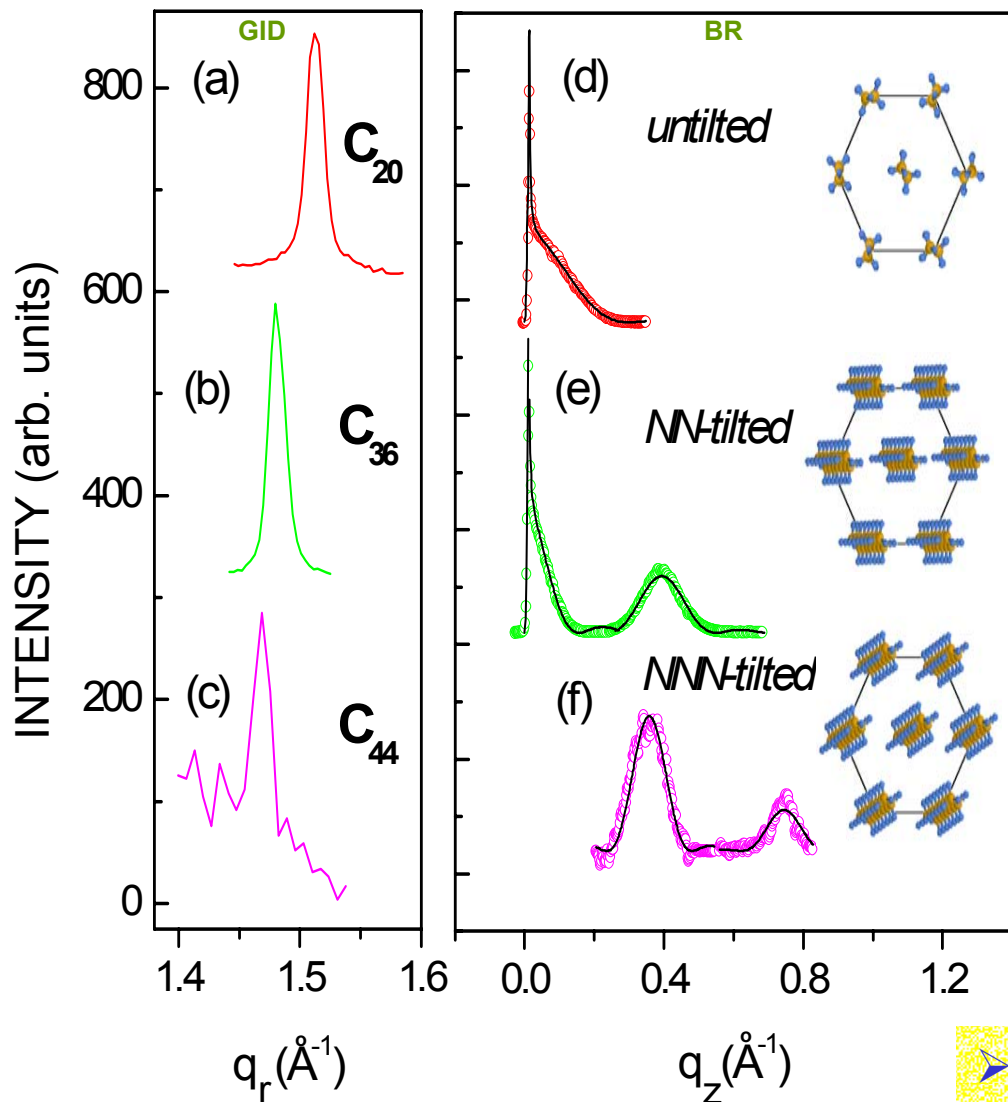
NN tilted

NNN tilted

Intermediate tilt



Alkanes: In-plane structure



X. Wu et al., *Science* **261**, 1018 (1993)
 B. Ocko et al., *Phys. Rev. E* **55**, 3164 (1997)

- In-plane order \Rightarrow quasi-2D crystal .
- Hexagonal packing.
- Three types: no tilt, NN tilt, NNN tilt.

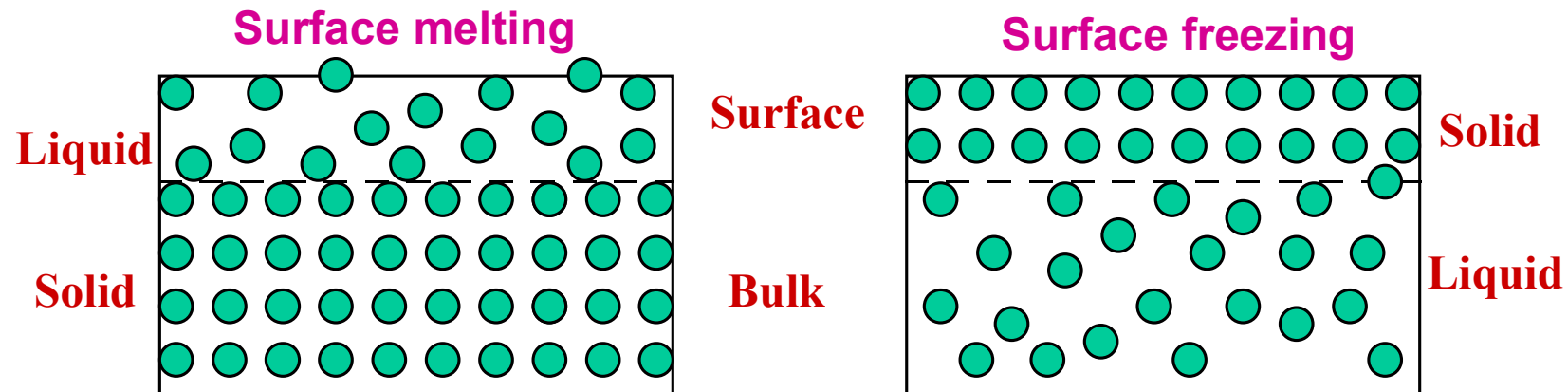


Surface Freezing

Statistical Mechanics

- Phase diagrams and boundaries depend on dimensionality
- For all materials $T_{\text{melt}}(2\text{D}) < T_{\text{melt}}(3\text{D})$

Molecules at the surface are less confined, have higher entropy, and hence melt at a lower temperature than in the bulk.



The general rule

Observed in:
 metals
 semiconductors
 molecular crystals
 ice etc.

Very rare

The only related effect : surface ordering in liquid crystals.
 (but order is smectic not crystalline)

Theory: entropic stabilization by large vertical fluctuations, possible at the surface but not in the bulk.

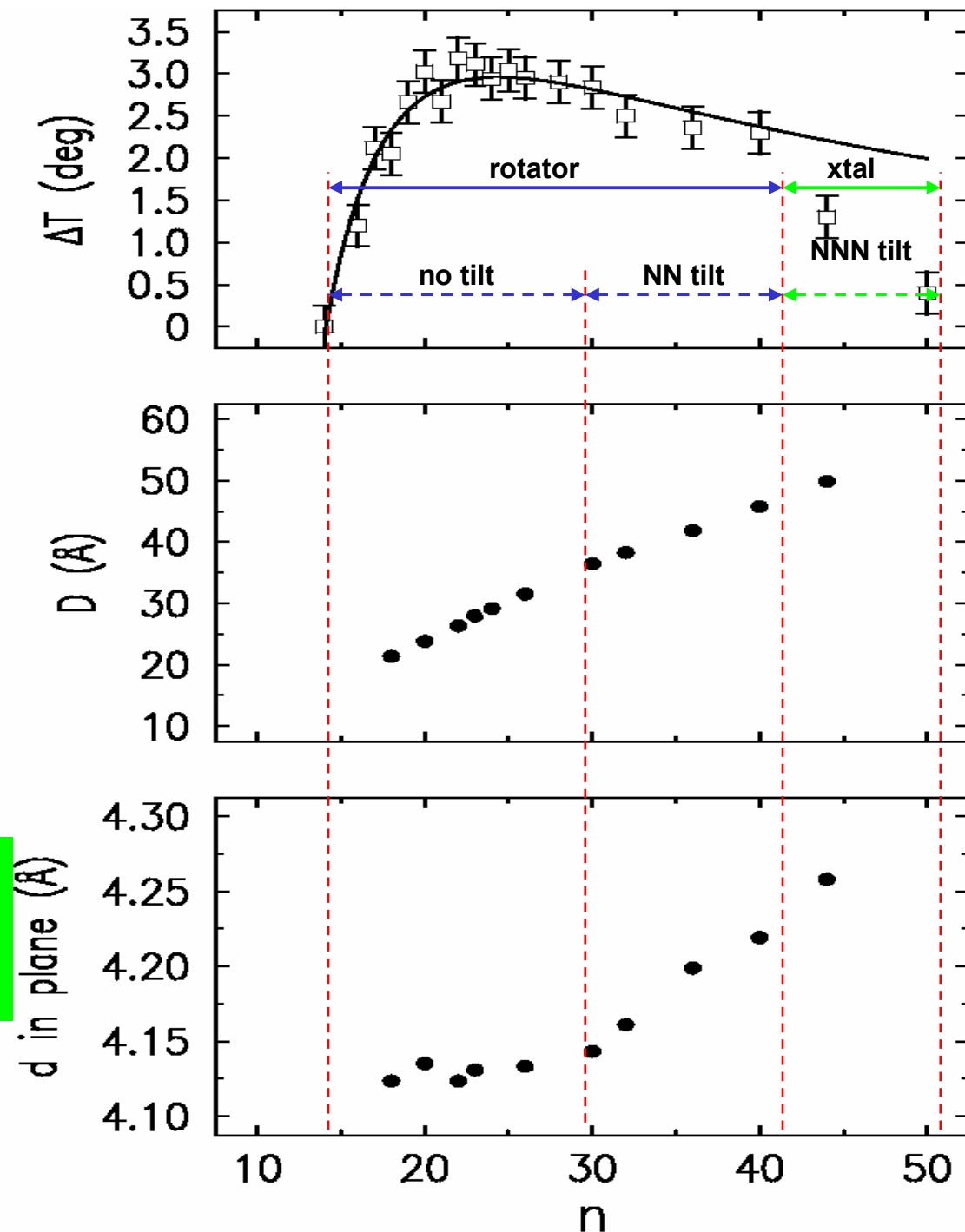
Tkachenko & Rabin, *Phys. Rev. Lett.* **76**, 2527 (1996)



Alkanes: 2D surface phase diagram

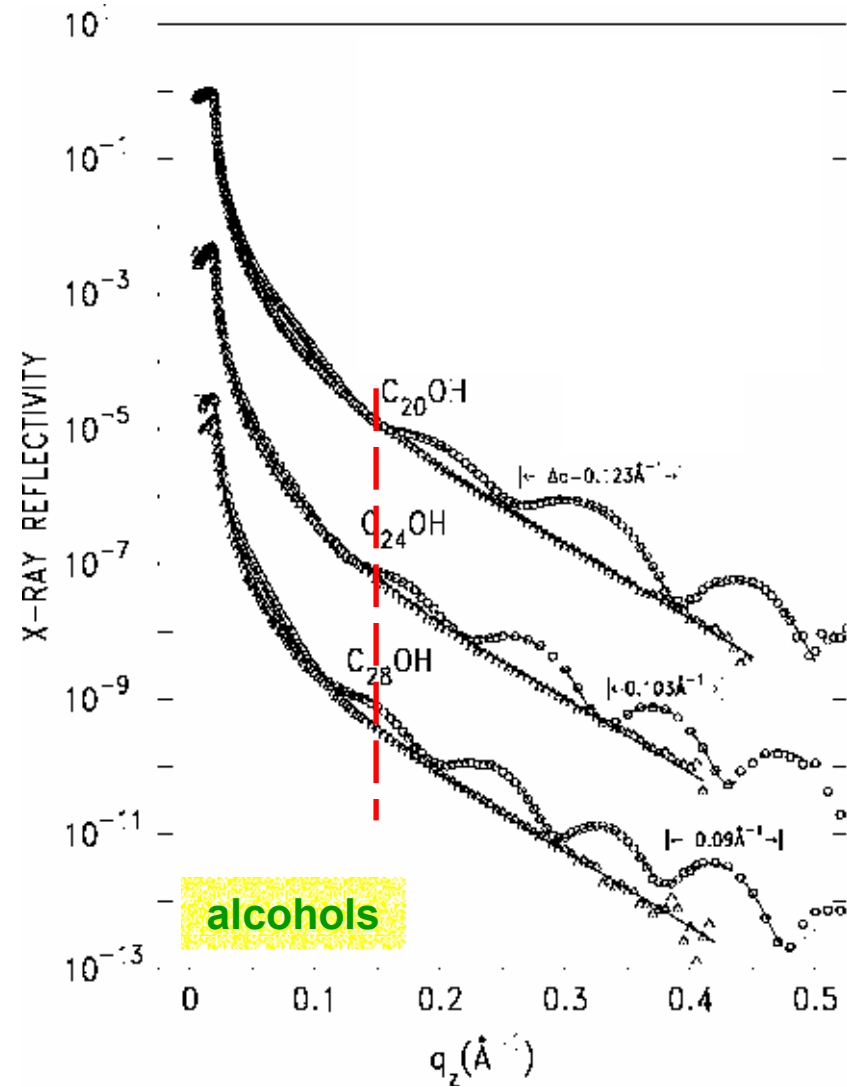
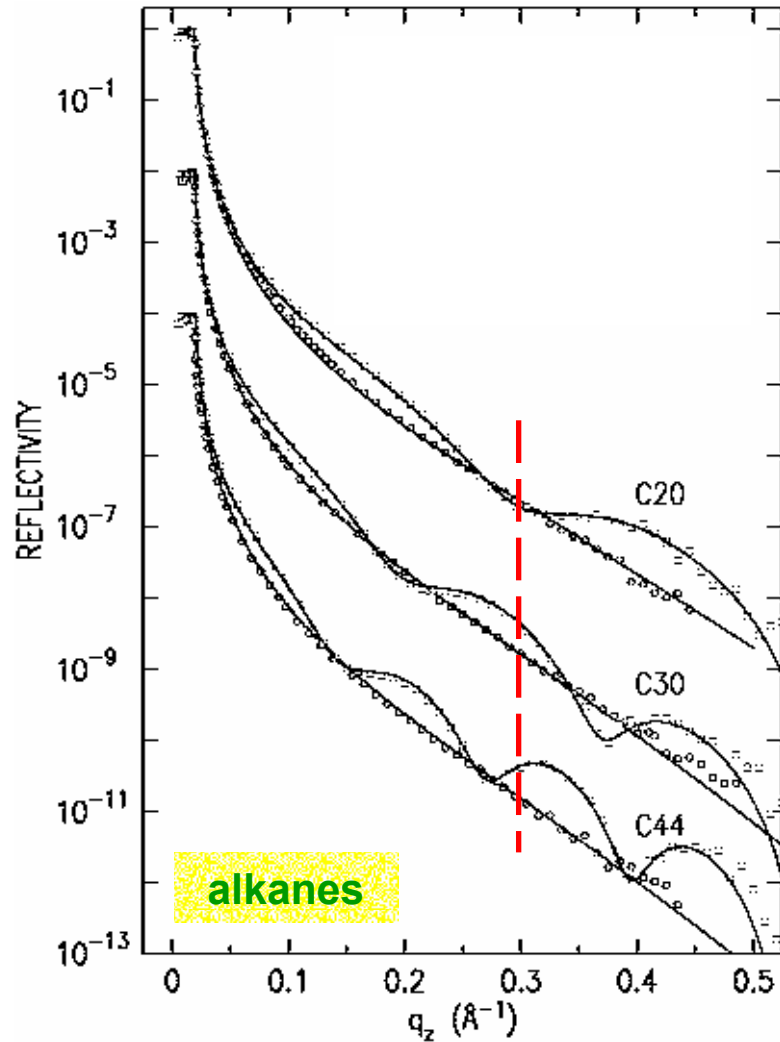
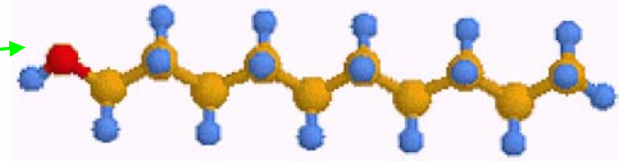
- ❖ Always a *monolayer*.
- ❖ Packing always hexagonal.
- ❖ No structure variations with T.
- ❖ Structure varies with n.
- ❖ Limited chain length range.
- ❖ Limited temperature range.

Does surface freezing occur in other molecules, or just in alkanes?



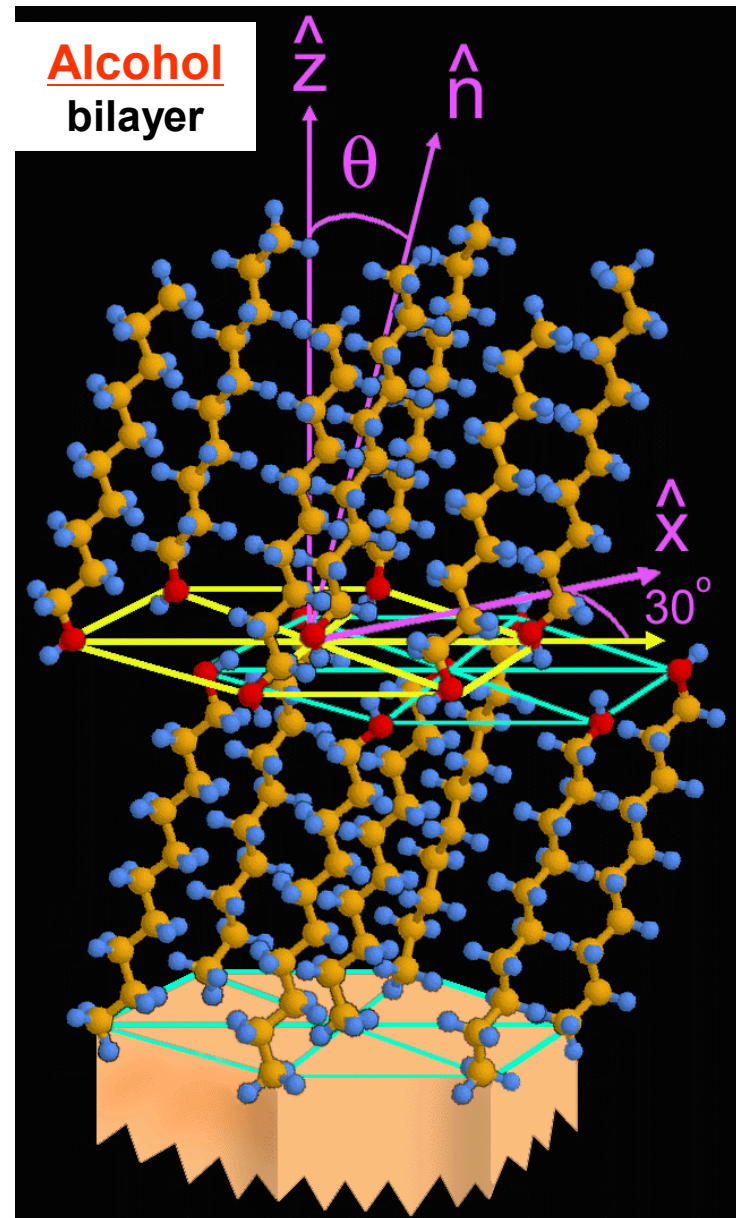
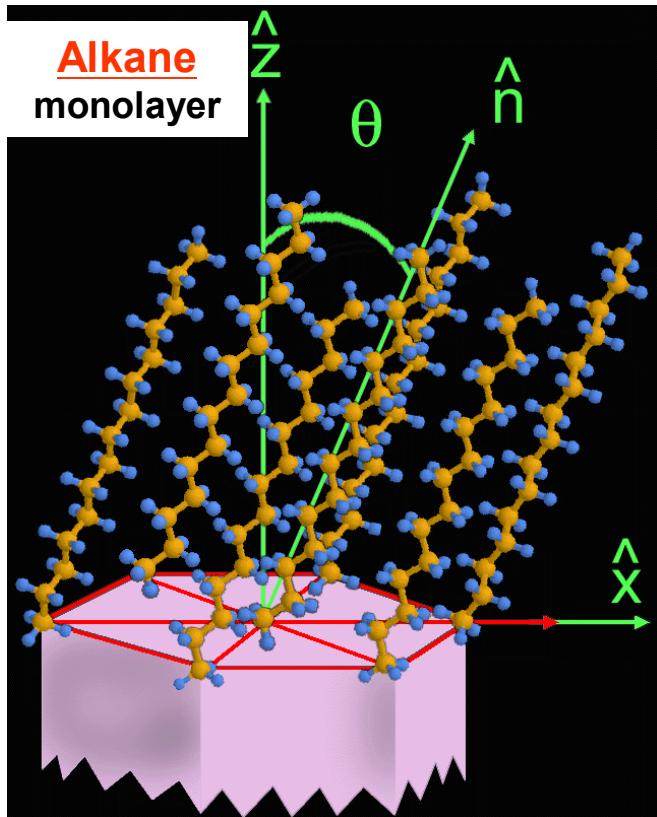
Surface Freezing in Alcohols (I)

OH headgroup, allows hydrogen bonding.



Surface Freezing in Alcohols

O. Gang et al.,
Phys. Rev. E
58, 6068 (1998)

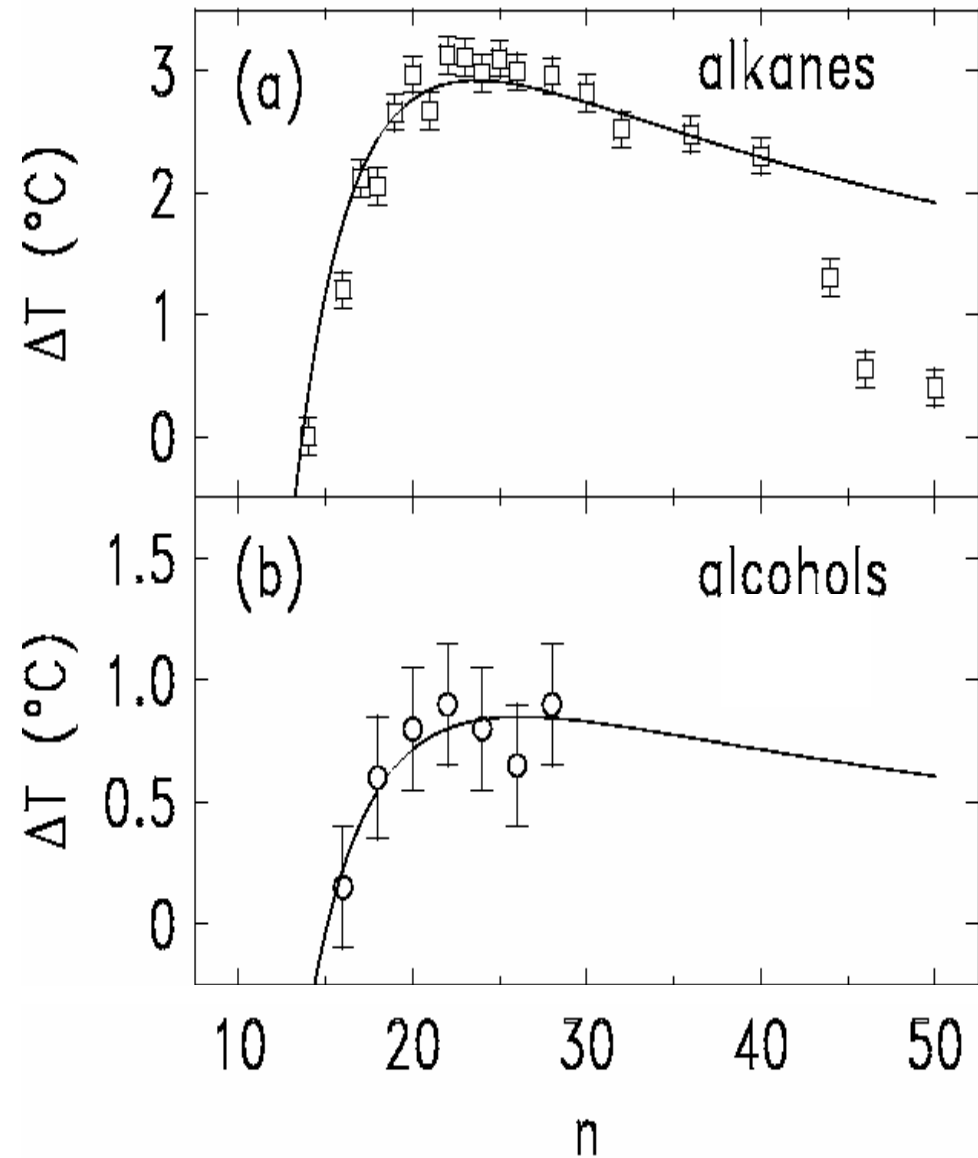
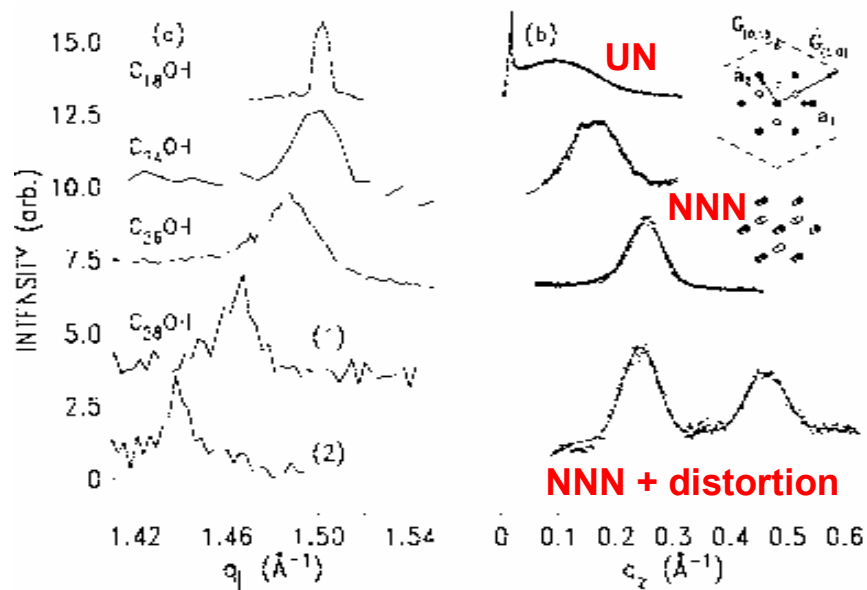


Surface Freezing in Alcohols(III)

- Only even alcohols show SF.
- T-range smaller than alkanes.
- n-range smaller than alkanes.
- Phases: UN → NNN → NNN+dist. (alkanes: UN → NN → NNN)

But....

- Max. SF layer thickness larger.
- T_S and T_F much higher.

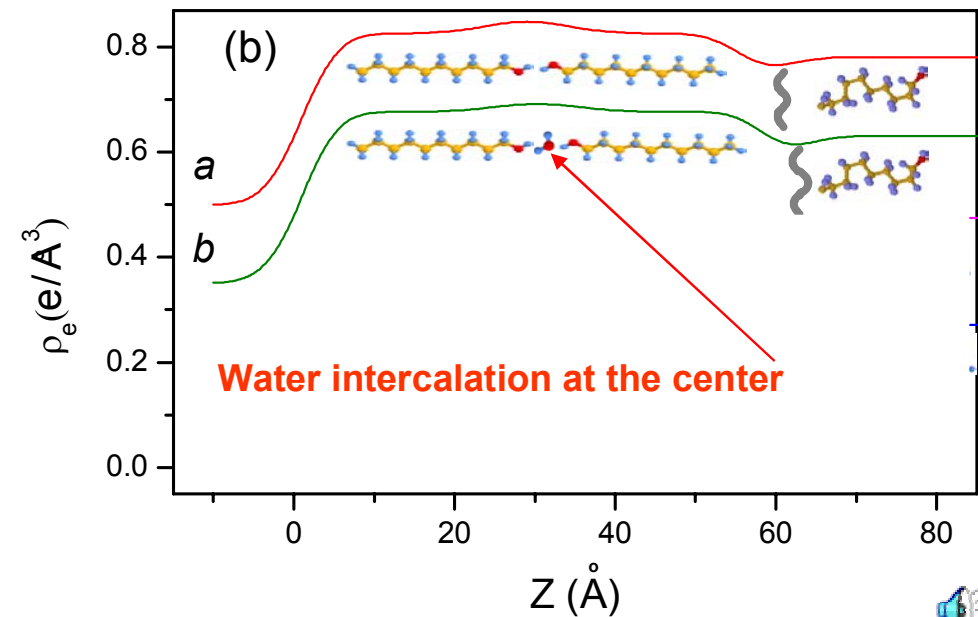
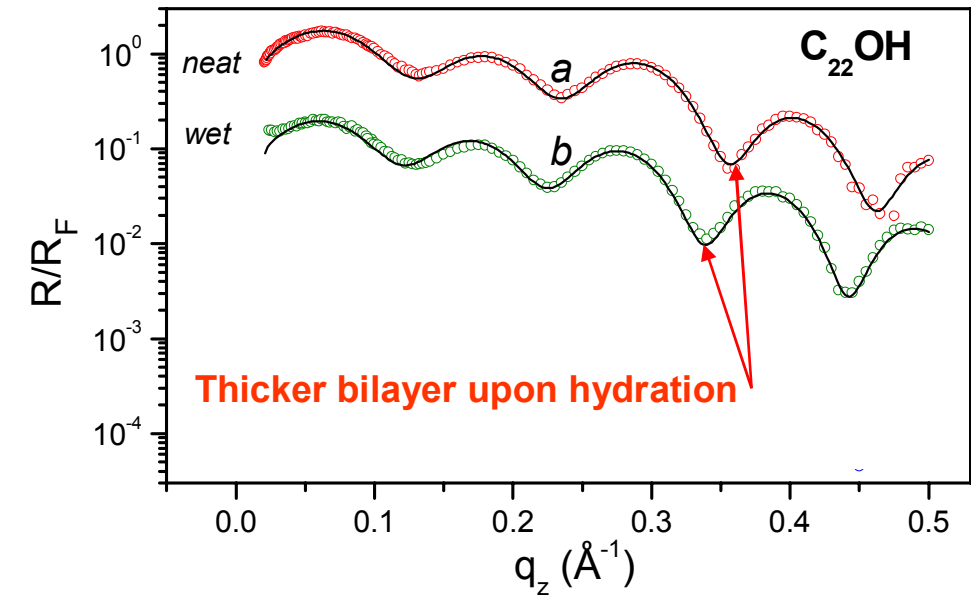
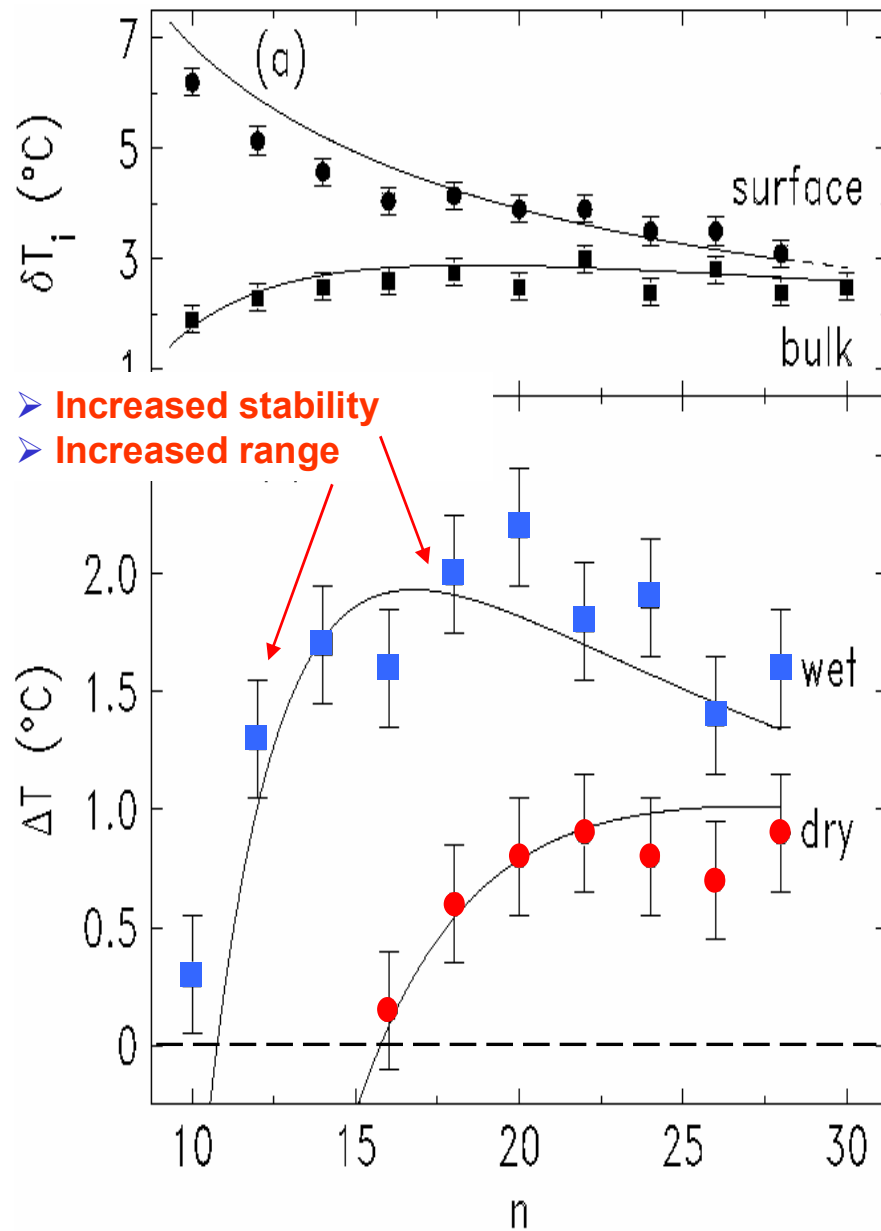


O. Gang et al., *Phys. Rev. E* **58**, 6068 (1998)



Alcohols: Straight or On the Rocks

O. Gang et al., *Phys. Rev. Lett.* **80**, 1264 (1998)



Liquid metals (I)

Unique properties

- two component fluid (ion jellium + quantum fluid)
- Ga: $0.50 T_m < \text{liquid range} < 8.3 T_m$
Largest of all liquids
- magnitude of surface tension and variation from metal to metal not explained by theory:

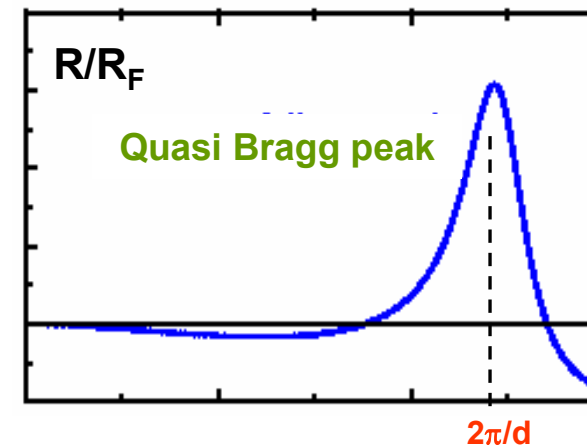
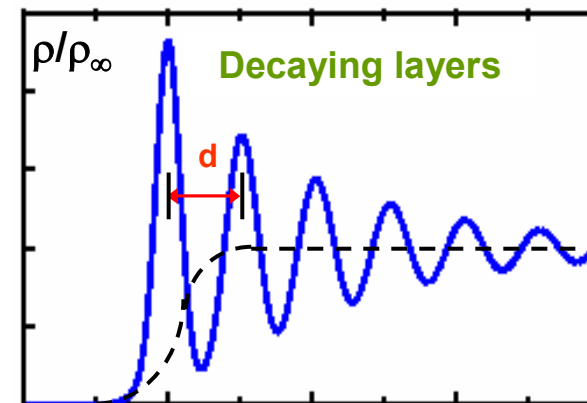
	γ	T_m	γ/T_m
Cs	70	301	0.23
W	2500	3655	0.68
Al	914	933	0.98
Hg	498	234	2.13
Ga	718	302	2.38
I ₂	38	380	0.1
NaCl	114	1076	0.11
SiO ₂	307	2073	0.15
Ar	13.1	84	0.16
H ₂ O	72.8	293	0.25

- pronounced supercooling in LM

How would these properties be reflected in the structure of the surface ?

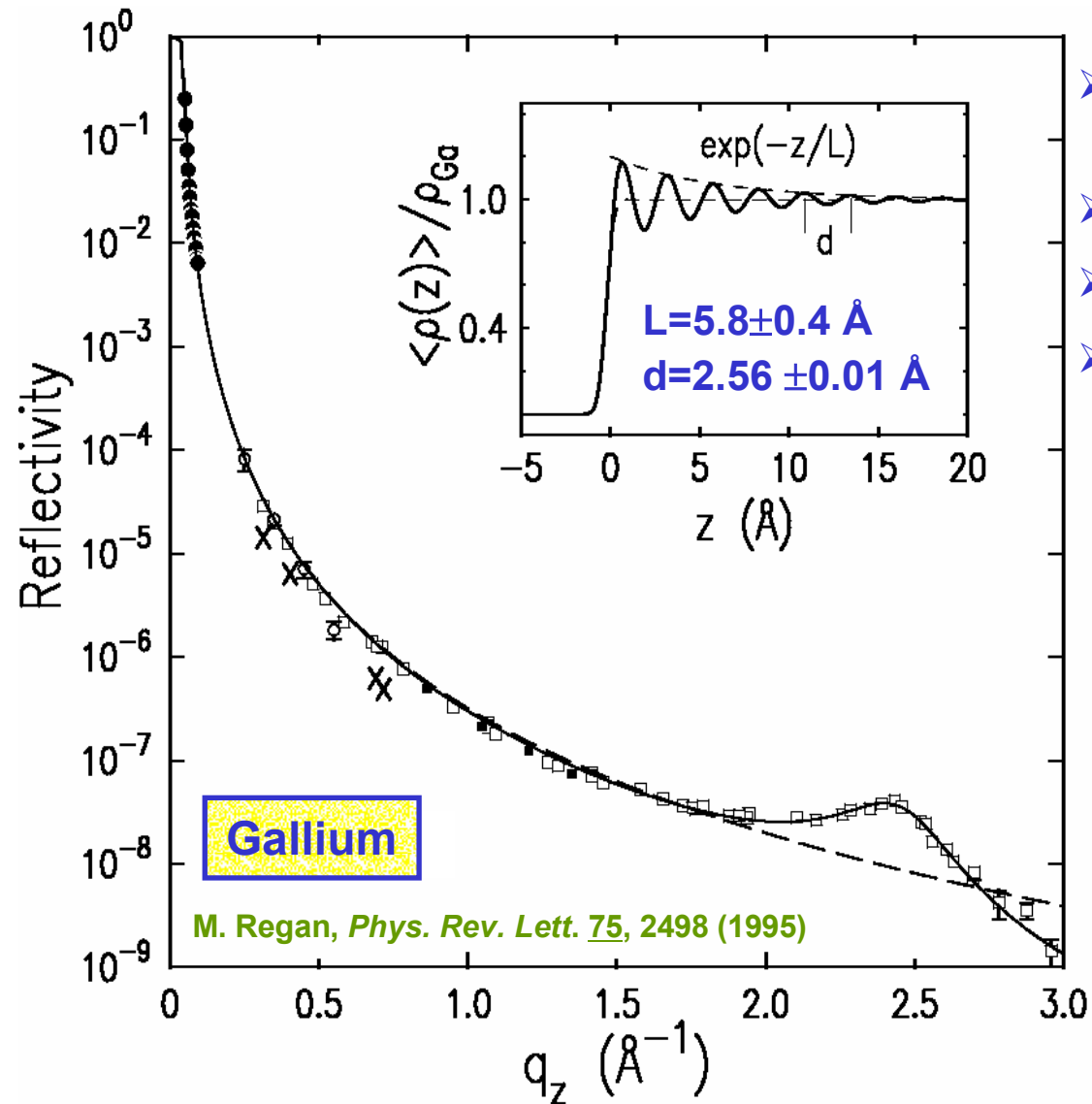
Surface layering, similar to atoms at a solid wall
Theory & simulations Rice & others (1960-1985)

Expected:



Liquid metals (II)

Observed:



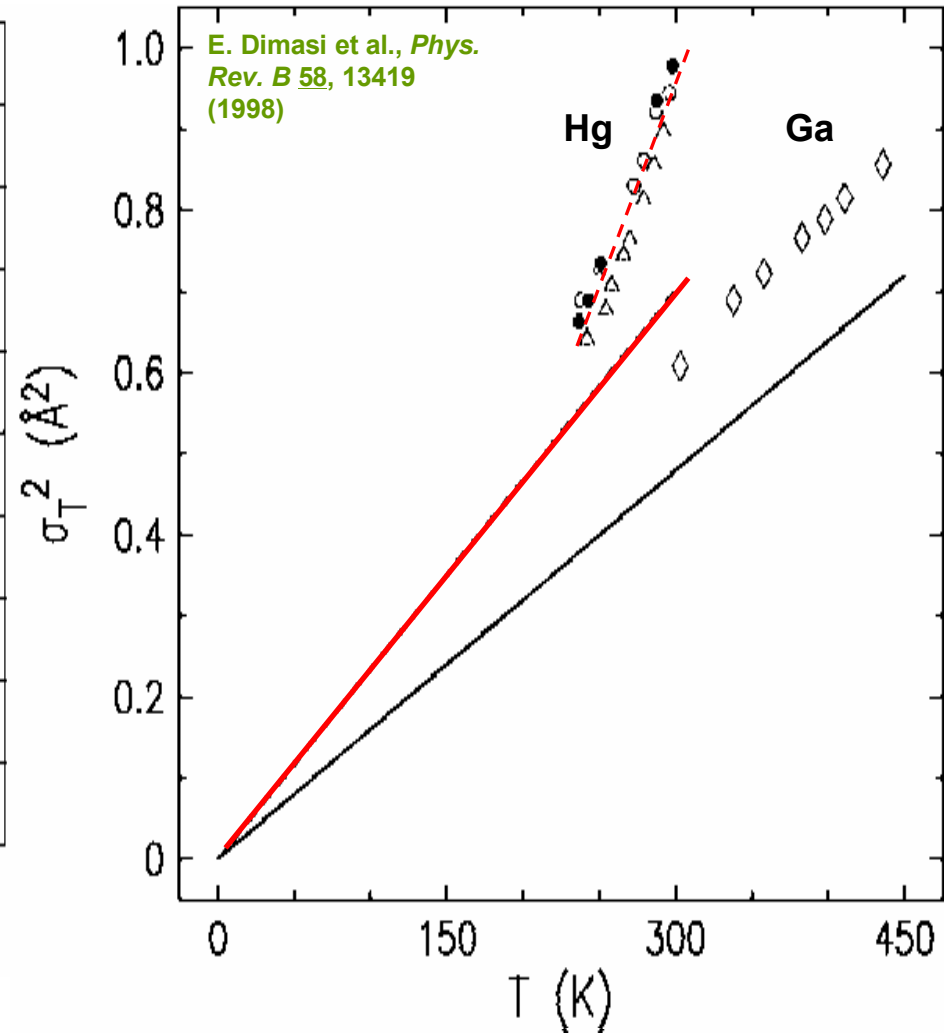
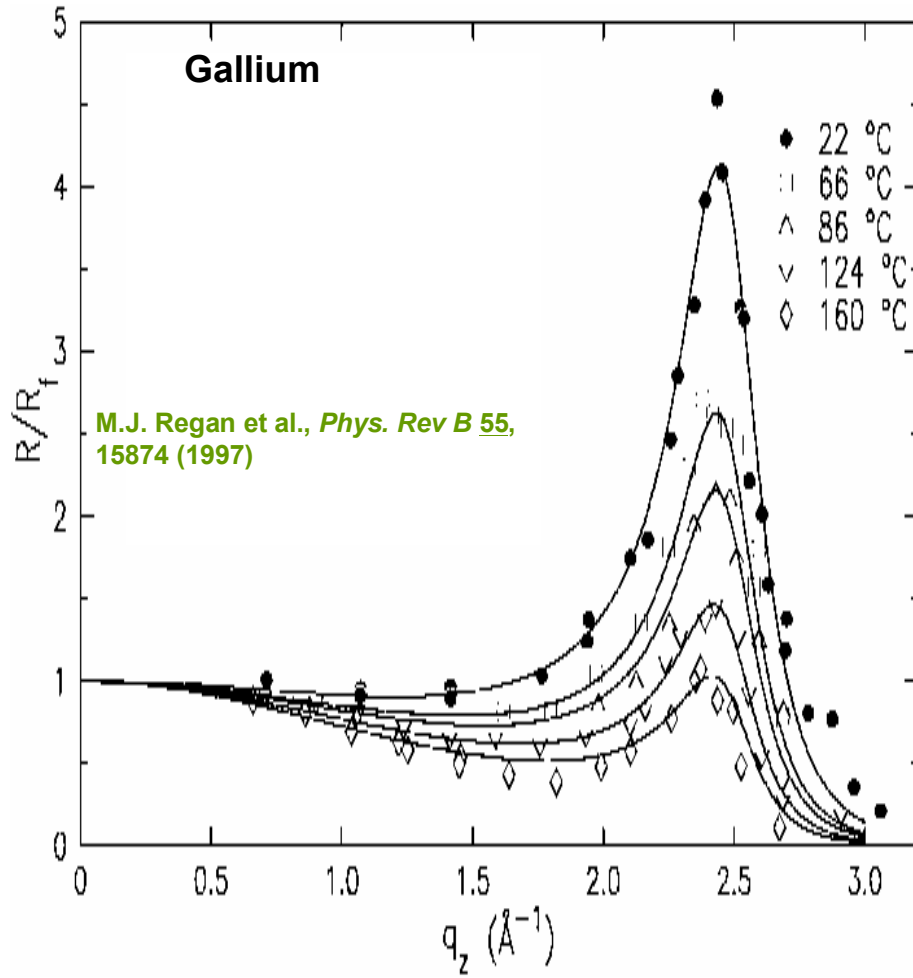
- First clear observation of layering (now also in Hg, In, Sn, alloys....).
- Roughness: 0.8 \AA vs. 3.2 \AA for water
- q_z - range: 3 \AA^{-1} vs. 0.7 \AA^{-1} for water.
- L at surface > L at bulk ! (dimers ?).



Liquid metals (III)

Does the layering interfere with CW ?

$$\sigma^2 = \sigma_0^2 + \frac{k_B T}{4\pi\gamma} \ln\left(\frac{q_{\max}^2}{q_{\min}^2}\right)$$



What was left out.....

Because of time limitaion many current studies were left out:

- ❖ The surface structure of van der Waals liquids (organic liquids etc.).
- ❖ The structure of liquid alloys.
- ❖ Wetting in binary liquid mixtures (long range, short range).
- ❖ Adsorbed Gibbs layers at the liquid surface.
- ❖ Overlayers on water: Langmuir films.
- ❖ Overlayers on metals: surface oxidation, organics monolayers on metals.
- ❖ The structure of the liquid-liquid interface.
- ❖ The structure of a solid-liquid interface.



Thanks

Water

- A. Braslau, B. Ocko, A. Weiss, P. Pershan (Harvard), J. Als-Nielsen, J. Bohr (Risø)

Liquid metals

- N. Maskil, H. Kraack (Bar-Ilan), M. Regan, H. Tostmann, P. Pershan (Harvard), O. Magnussen, E. DiMasi, B. Ocko (BNL)

Surface Freezing

- O. Gang, H. Kraack, E. Sloutskin (Bar-Ilan), X. Wu, E. Sirota (Exxon), B. Ocko (BNL)

\$\$\$\$\$ (actually ccc)

Israel: U.S.-Israel BSF, ISF, Exxon
U.S. :DOE, NSF

Beamtime:

NSLS, Brookhaven National Laboratory
APS, Argonne National Laboratory
HASYLAB, Hamburg, Germany
ESRF, Grenoble, France



One of my previous talks
at the University of

