

Super-bunch Hadron Colliders

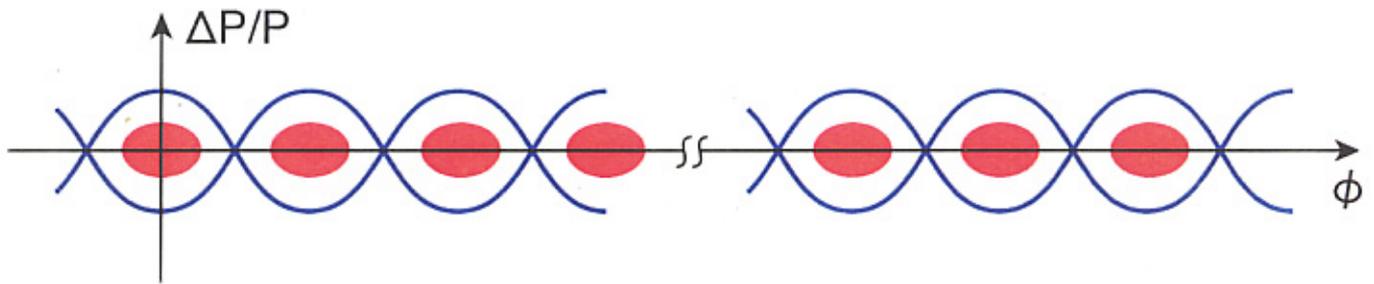
RPIA2002, 29 October 2002

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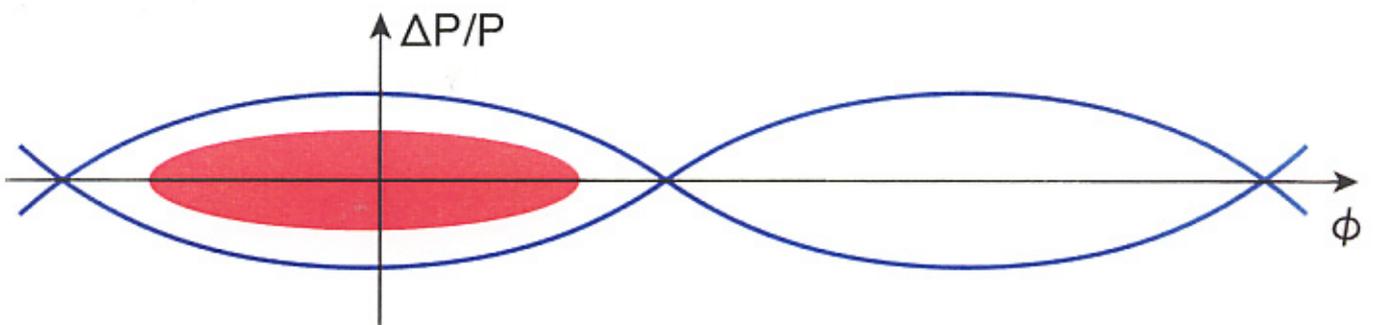
1. Introduction
2. What is a Super-bunch?
3. Milestone toward a Super-bunch Hadron Collider
4. Characteristics
 - Bunch formation
 - Collision scheme and beam-beam tune spreads
 - Luminosity
5. Possible parameters
6. Beam physics issues
 - Long range beam-beam effects
 - Coherent instability
7. Machine issues
 - Heat Load
 - IR design
8. R&D time table
9. Summary

RF bunch & Super-bunch

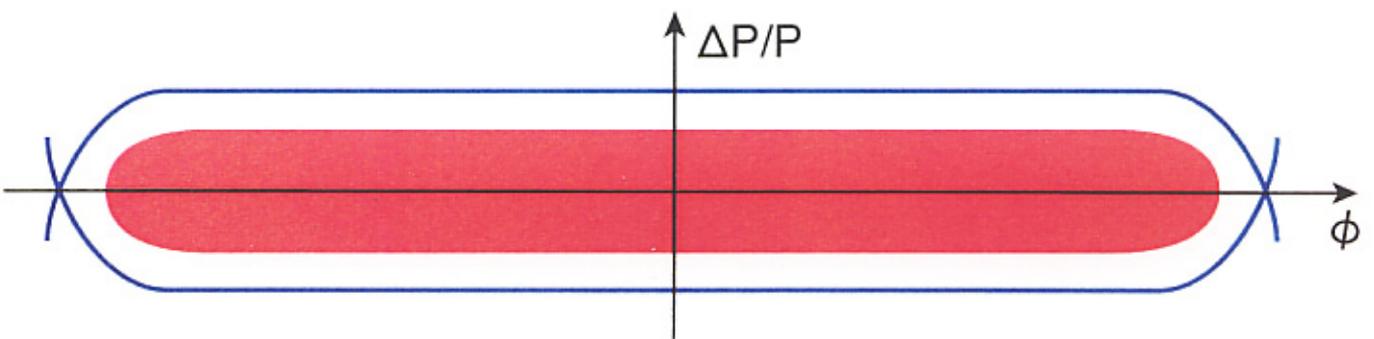
(1) Present higher harmonic RF bunch



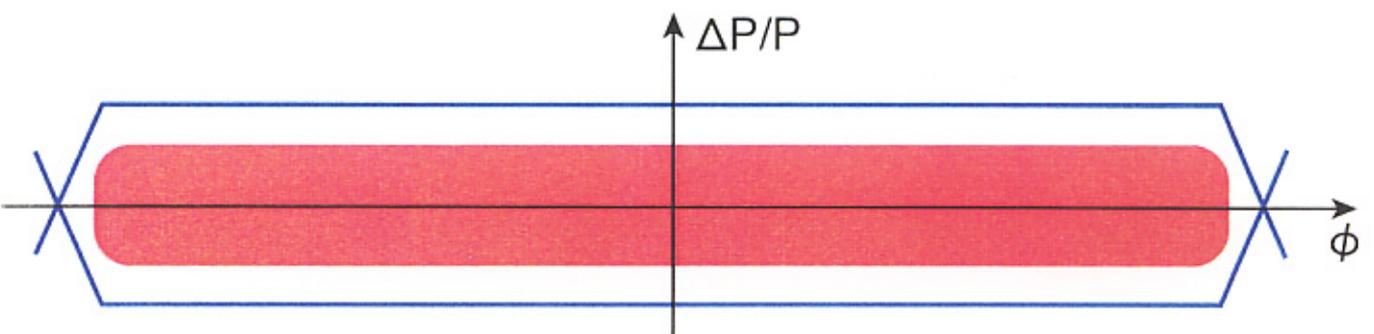
(2) Low harmonic RF Super-bunch



(3) Super-bunch in an RF barrier bucket



(4) Super-bunch in a Step-barrier bucket



Super-bunch

	Type of Super-bunch		
	Low harmonic RF bunch	Barrier bucket bunch	
		RF barrier	Step barrier
Required devices	low harmonic cavity and low freq. power source	● low Q cavity and multiple RFs or amplified pulse voltage	induction cavity
Characteristics			
Advantage	<ul style="list-style-type: none"> ● well developed technology ● small RF voltage bucket height $\approx \left[\frac{V}{h}\right]^{1/2}$ 	<ul style="list-style-type: none"> ● already demonstrated ● easy bunch formation 	<ul style="list-style-type: none"> ● easy bunch formation by only controlling a trigger timing ● uniform line density
Disadvantage	<ul style="list-style-type: none"> ● limited available space in the phase space ● highest line density at the bunch center ● slow synch. osci. 	<ul style="list-style-type: none"> ● no acceleration ● slow synch. osci. 	<ul style="list-style-type: none"> ● not demonstrated yet ● slow synch. osci.
Remarks	<ul style="list-style-type: none"> ● may need minor changes for bunch formation in the upstream ● merging process? 	<ul style="list-style-type: none"> ● good exercise for Step barrier beam handling 	<ul style="list-style-type: none"> ● needs modification for bunch-formation in the upstream accelerators

Milestone toward Super-bunch Hadron Colliders

Date	Authors or Institute	Pub. or Presentation	Remarks
Early 70's	CERN		Demonstration of the first continuous p-p beam collider (ISR)
1973	E.Keil	<i>Nucl. Inst. Meth.</i> 113, 333 (1973)	Luminosity, beam-beam tune-shift calculation for coasting beam collision
1983, March	J.Griffin et al.	PAC1983	Proposal of RF barrier bucket
1999, July	K.Takayama and J.Kishiro	ν FACT'99 <i>Nucl. Inst. Meth.</i> 451, 304 (2000)	Concept of Induction Synchrotron
2001, March	K.Takayama et al.	KEK Preprint 2000-147 (2001)	First proposal of SHC concept
2001, June - July	R.Yamada, Super-bunch sub working-group	PAC2001 Snowmass 2001	Proposal of VLHC schemes with Super-bunch option Beam physics
2002, April	K.Takayama, J.Kishiro, M.Sakuda, Y.Shimosaki, and K.Wake	<i>Phys.Rev. Letts</i> 88, 144801 (2002)	Concept and Beam physics of SHC (Luminosity, tune-spread, inclined crossing)
2002, June	F.Zimmermann	EPAC2002, in Proc., 25 (2002)	e-p Instability in Super-bunch option
2002, October	F.Ruggiero,R.Garoby, F.Zimmermann et al.	LHC Project Report	Feasibility study of Super-bunch option in LHC upgrade

ISR

ISR Parameter List

Max. total energy	E_{\max}	28 GeV
Average radius	R	150 m
<u>Intersection angle</u>	α	15°
No of magnet periods	N	48
No of superperiods	S	4
No of intersections		8
Long s.s. length		16.8 m
Q value	Q	8.75
Max. horizontal β value	$\beta_H \max$	41 m
Max. vertical β value	$\beta_V \max$	51 m
Max. momentum compaction	$\alpha_p \max$	2.3 m
No of magnets per ring		132
Max. field	B_0	1.2 T
Bending radius	ρ	78.5 m
Profile parameter	n/ρ	3 m^{-1}
Gap height		0.1 m
Harmonic number	h	30
R.F. volts per turn	50 V to	20 kV
Design pressure		10^{-9} torr
Vac. chamber dimensions		$16 \times 5.2 \text{ cm}^2$

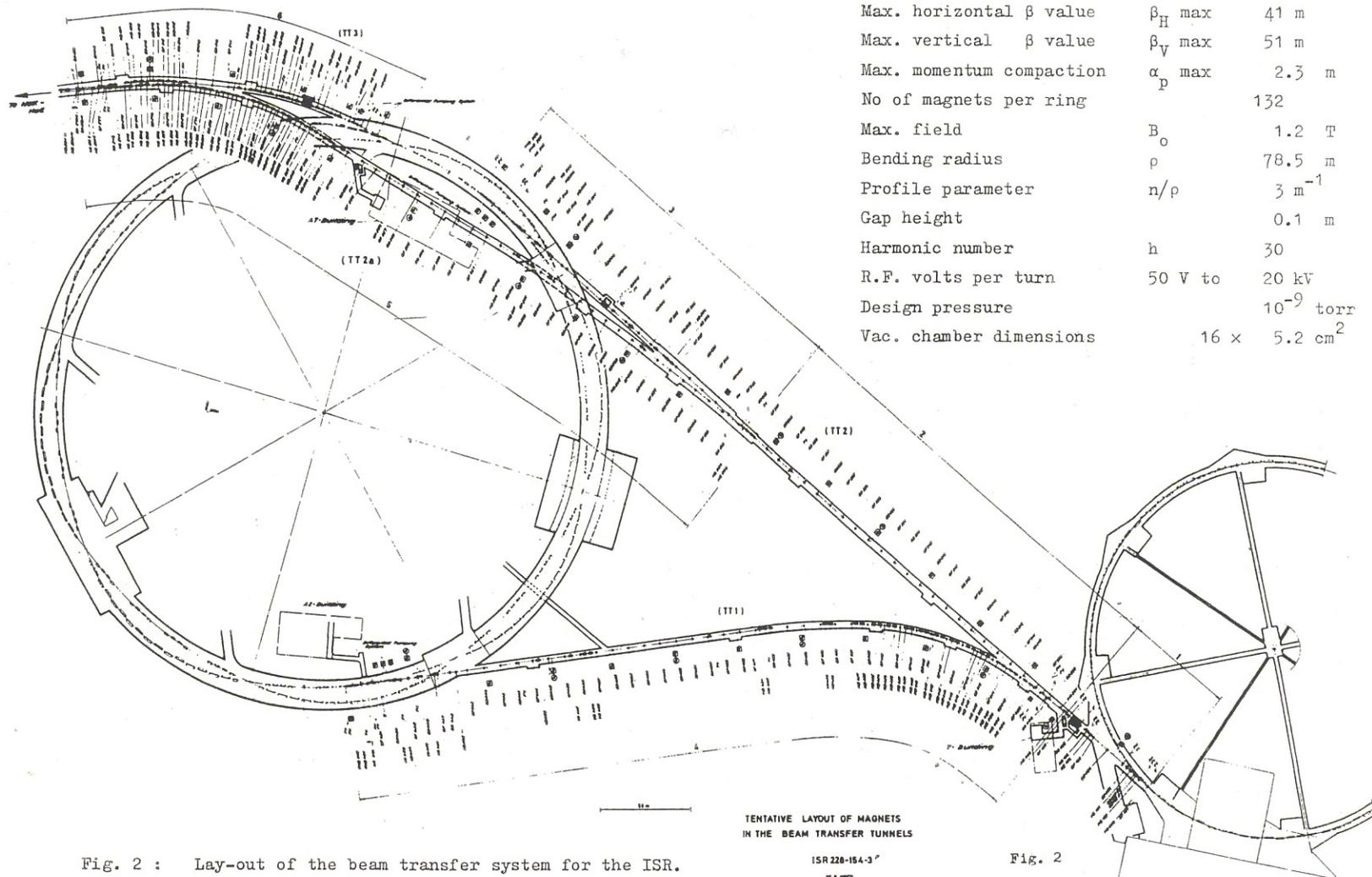
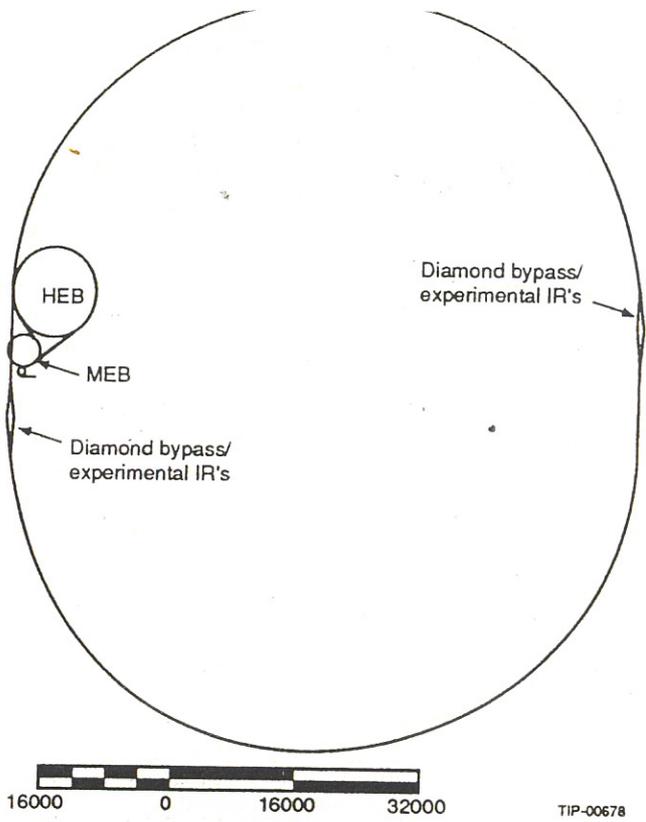


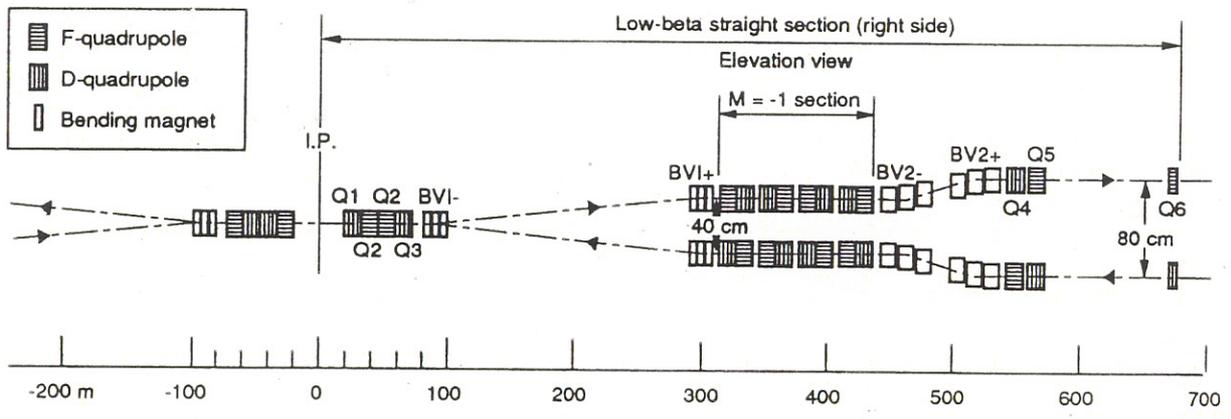
Fig. 2 : Lay-out of the beam transfer system for the ISR.

Fig. 2

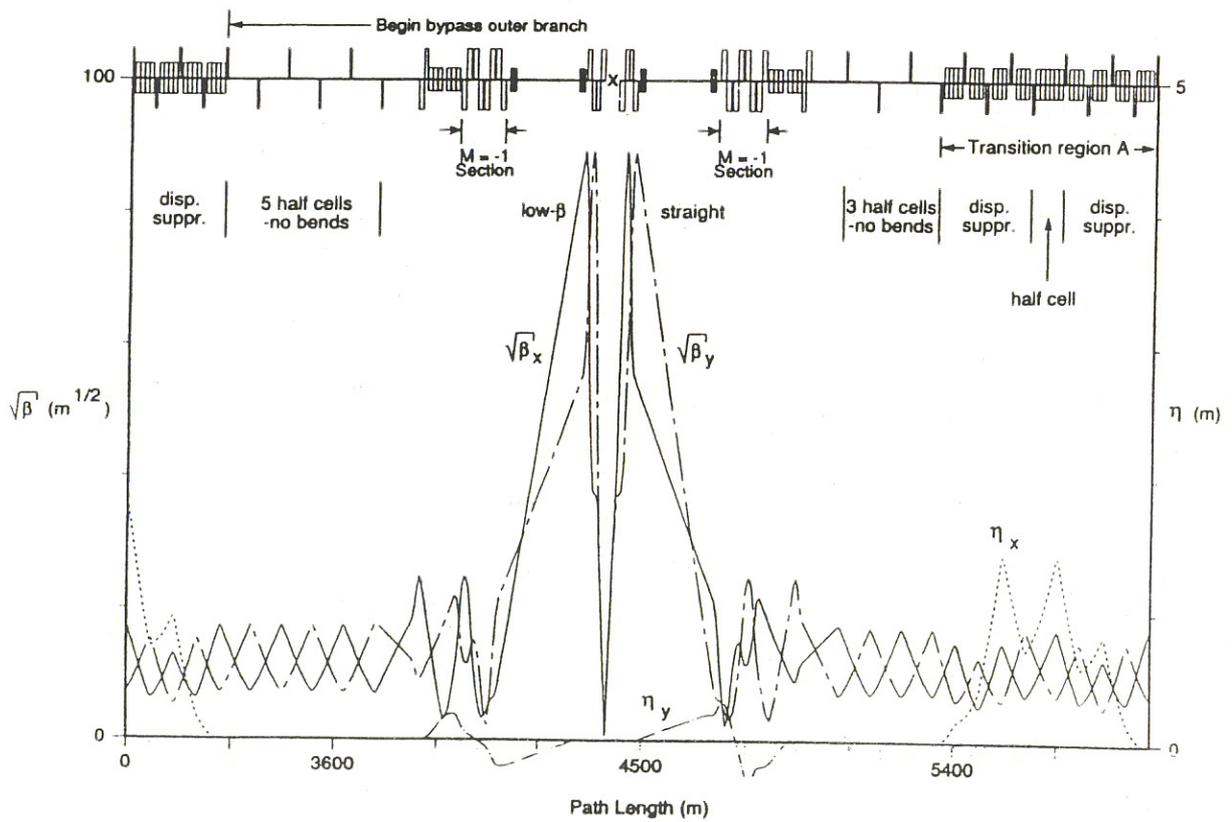
SSC



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Limit or Overview of Conventional Hadron Colliders

Luminosity

$$L = F \frac{k_b N_b^2 f_{rev} \gamma}{4\pi \epsilon_n \beta^*}$$

k_b : number of bunches

N_b : number of protons / bunch

f_{rev} : revolution frequency

ϵ_n : normalized emittance

β^* : betafunction at the IP

F : reduction factor with crossing Φ

Beam physics limit

Space-charge limit in upstream accelerators:

$$\Delta v \propto N_b / \epsilon_n \leq 0.25$$

Beam-beam limit:

$$\xi = \frac{N_b r_0}{4\pi \epsilon_n} \leq 0.004 / \text{IP (empirical)}$$

Cryogenetic limit

Synchrotron radiation limit:

$$P_{rad} \propto k_b N_b \leq \text{a few watts / m}$$

Time resolution requirement from a detector

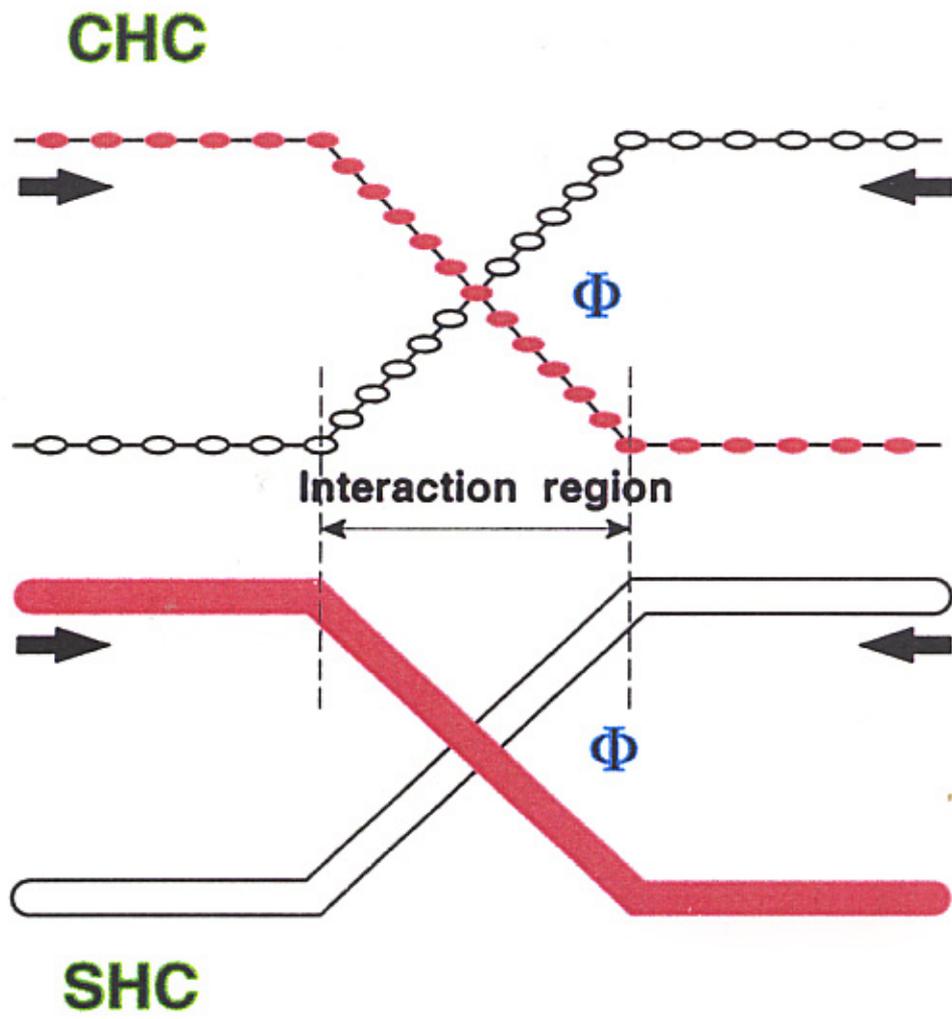
Bunch spacing limit: $d \geq 5m$

Beam occupation ratio

$$\kappa = \frac{\sqrt{2\pi} \sigma_s k_b}{C_0} \quad (\sigma_s: \text{rms bunch size})$$

= 2% for LHC, 1–3% for VLHC

Crossing with Angle

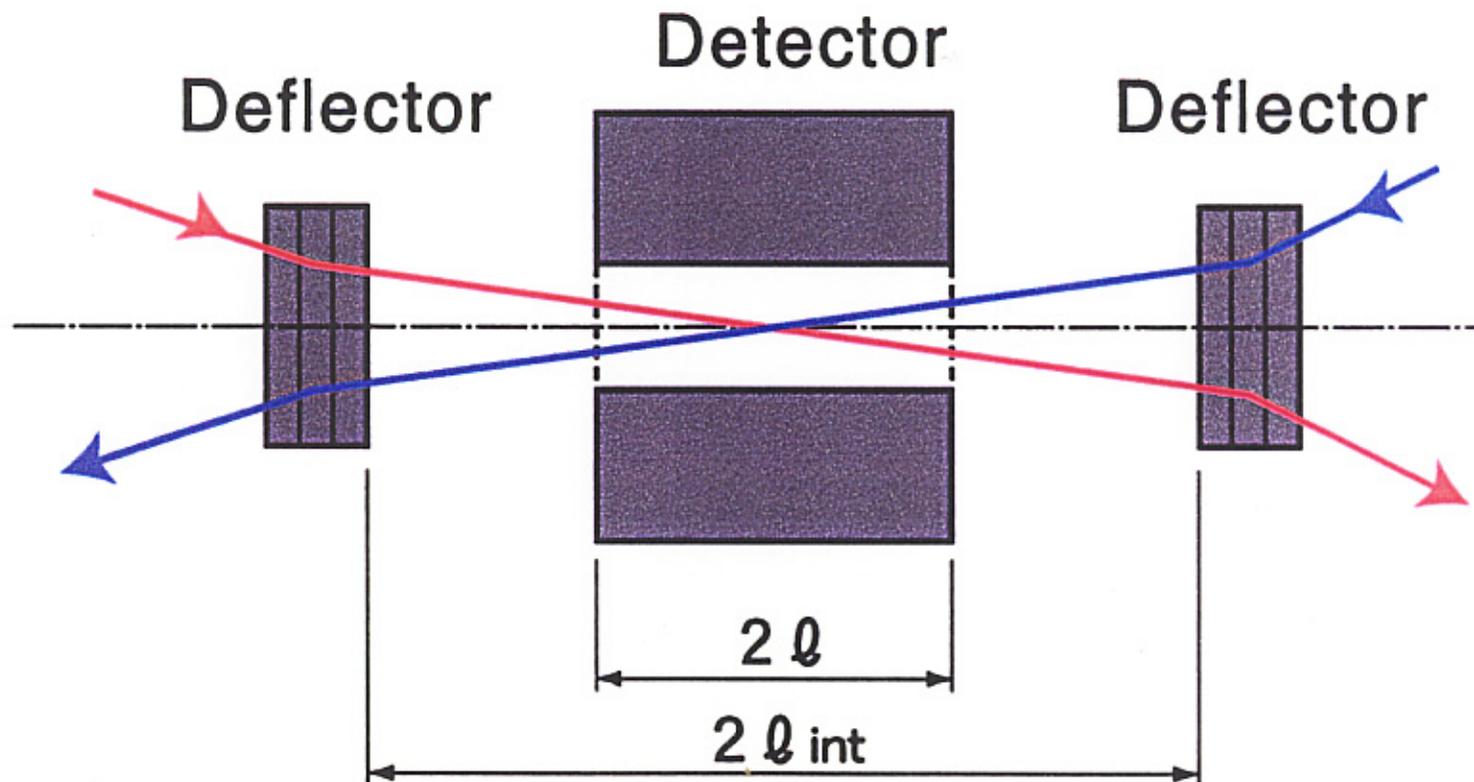


Big Questions

- How a long bunch (super-bunch) with the **same local intensity** as that of conventional hadron colliders (CHC) is generated?
- What happens in collision between such super-bunches?
- **Which collision scheme** is possible with super-bunches?
- What machine parameters are assumed?
- **Obstacles** can be overcome or not?

Preliminary results for case study at KEK and FNAL have been published in *Phy. Rev. Lett.* 88, 144801 (2002) and presented at Snowmass 2001 and at PAC2001. In addition, CERN has started their feasibility study as an upgrade plan of LHC in this early spring, where a low harmonic RF super-bunch is assumed. F.Zimmermann will describe about its details at this workshop.

INTERACTION REGION



Beam-beam tune shift in the SHC scheme

- Beam-beam tune-shift can be analytically evaluated by manipulating the 0-th harmonics of the Fourier components in the beam-beam perturbation term.
- The tune-shift normalized by the tune-shift ξ in the head-on collision of the CHC scheme is given in the form,

$$\frac{(\Delta v_x)_{\Phi}^{SHC}}{\xi} = \frac{8\beta^* \varepsilon_n}{\sigma_s \gamma} \int_0^{l_{int}} \frac{1+s^2/(\beta^*)^2}{\Phi^2 s^2} \left[1 - \exp\left(-\frac{\gamma \Phi^2 s^2}{2\varepsilon_n \beta^* (1+s^2/(\beta^*)^2)}\right) \right] ds \quad (1)$$

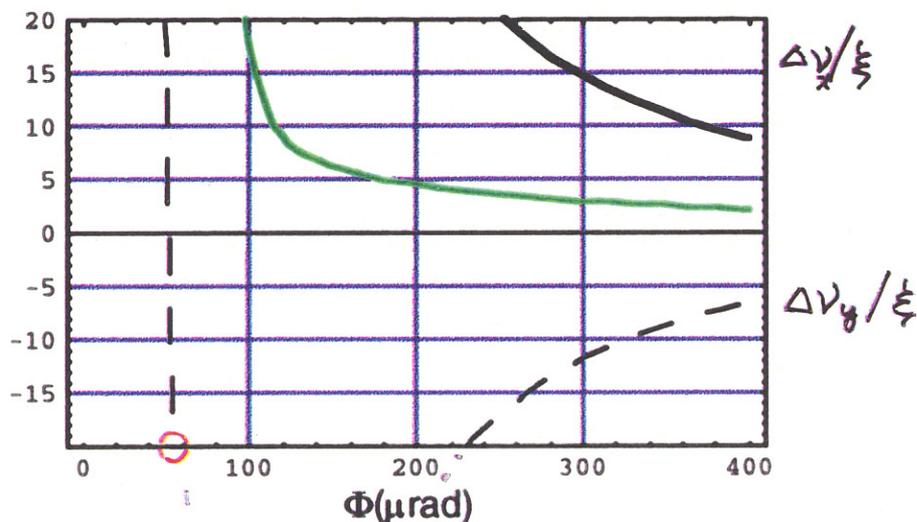
$$\frac{(\Delta v_y)_{\Phi}^{SHC}}{\xi} = \frac{8}{\sigma_s} \int_0^{l_{int}} \exp\left(-\frac{\gamma \Phi^2 s^2}{2\varepsilon_n \beta^* (1+s^2/(\beta^*)^2)}\right) ds - \frac{(\Delta v_x)_{\Phi}^{SHC}}{\xi} \quad (2)$$

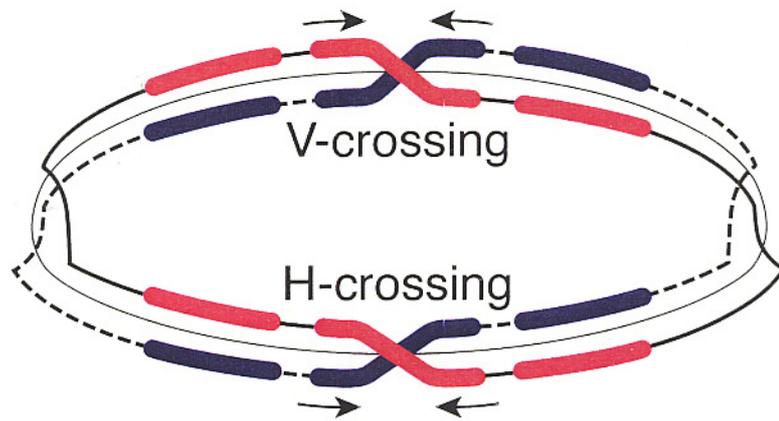
where crossing in the vertical direction is assumed and $2l_{int}$ is a size of the interaction region, $2l \ll 2l_{int} \ll \sigma_{sb}$.

- In the limit of $\Phi = 0$, $2l_{int} = \sigma_s/2$, Eqs. (1), (2) become unity.

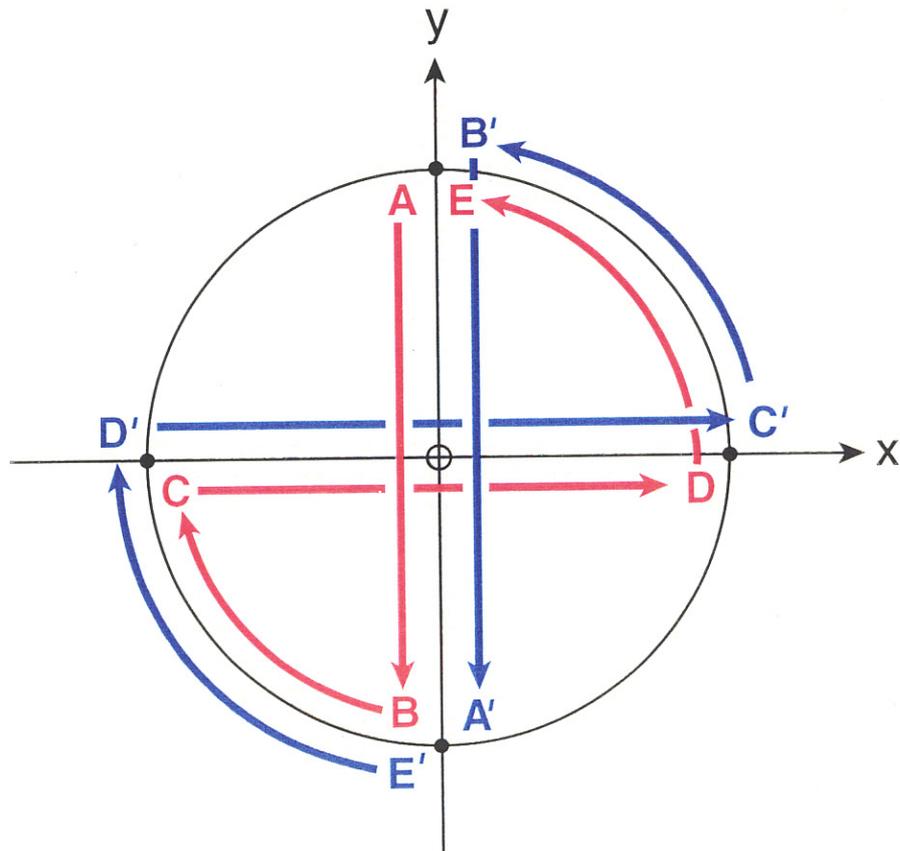
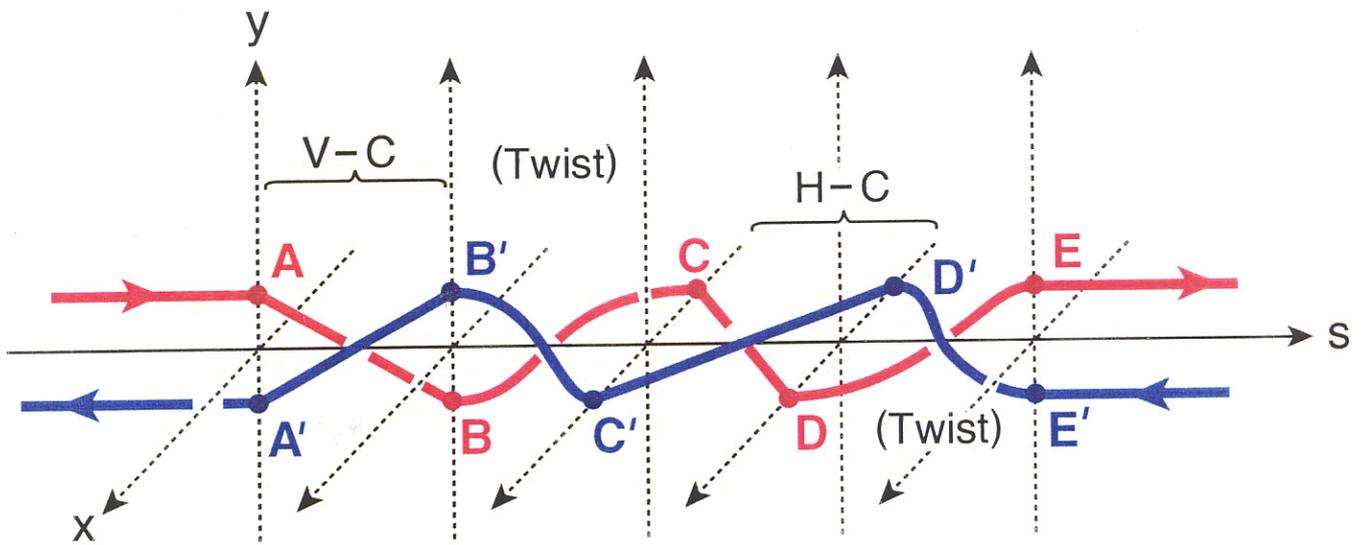
The numerical values for both directions are shown as functions of the crossing angle Φ below.

Black: horizontal, dash: vertical, green: sum



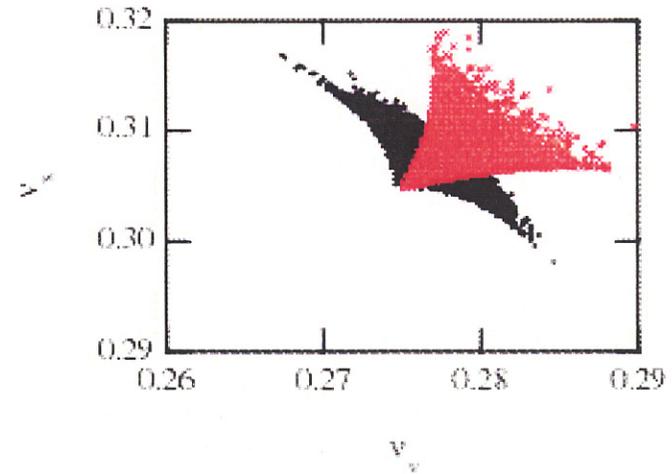
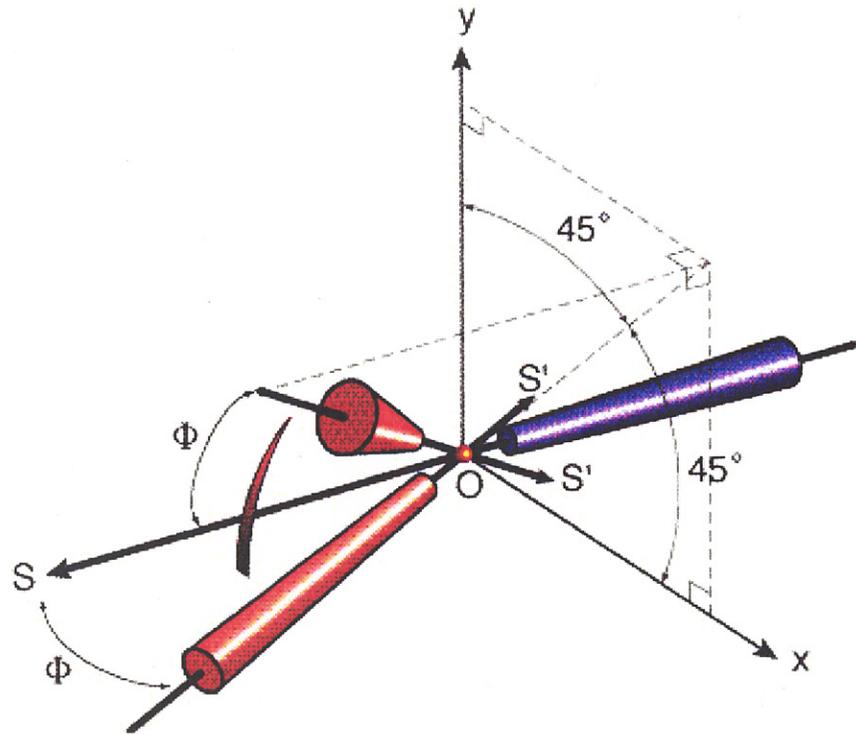


Hybrid Crossing (Mixed X-Y Crossing) in the same S.S.



Inclined Crossing & Beam-beam Tune Spread

For a case of LHC



Black: Hybrid crossing
(Vertical cross at North IR and horizontal cross at South IR)
Red: Inclined hybrid crossing

Luminosity in the SHC

$$L_{SHC}(\Phi, \ell) = 4 \frac{(k_{sb} \sigma_{sb})}{(k_b \sigma_s)} \frac{F_{SHC}(\Phi, \ell)}{\sigma_s F_{CHC}(\Phi')} L_{CHC}(\Phi')$$

where k_{sb}, k_b : number of superbunches, RF bunches per beam

σ_{sb} : superbunch length (full)

$\sigma_s = \sqrt{2\pi} \sigma_s$ (σ_s : rms RF bunch length)

Φ, Φ' : collision angle for SHC and CHC

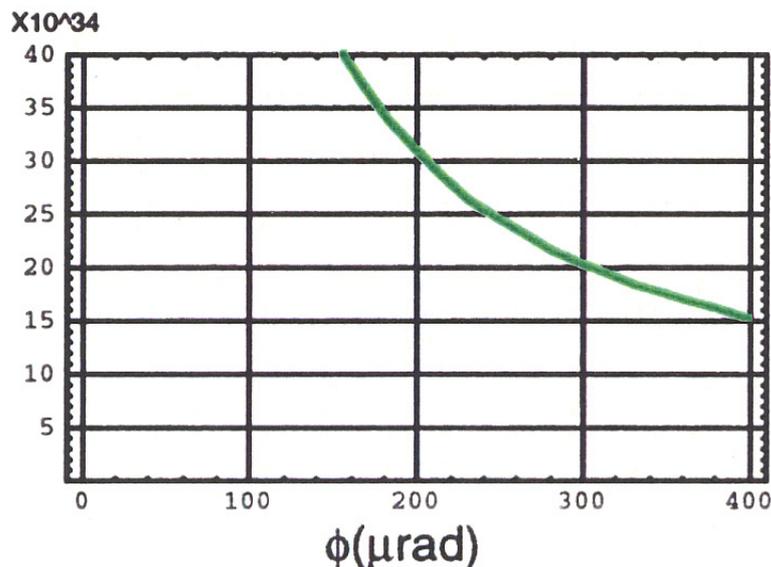
2ℓ : size of detector region

form factor:

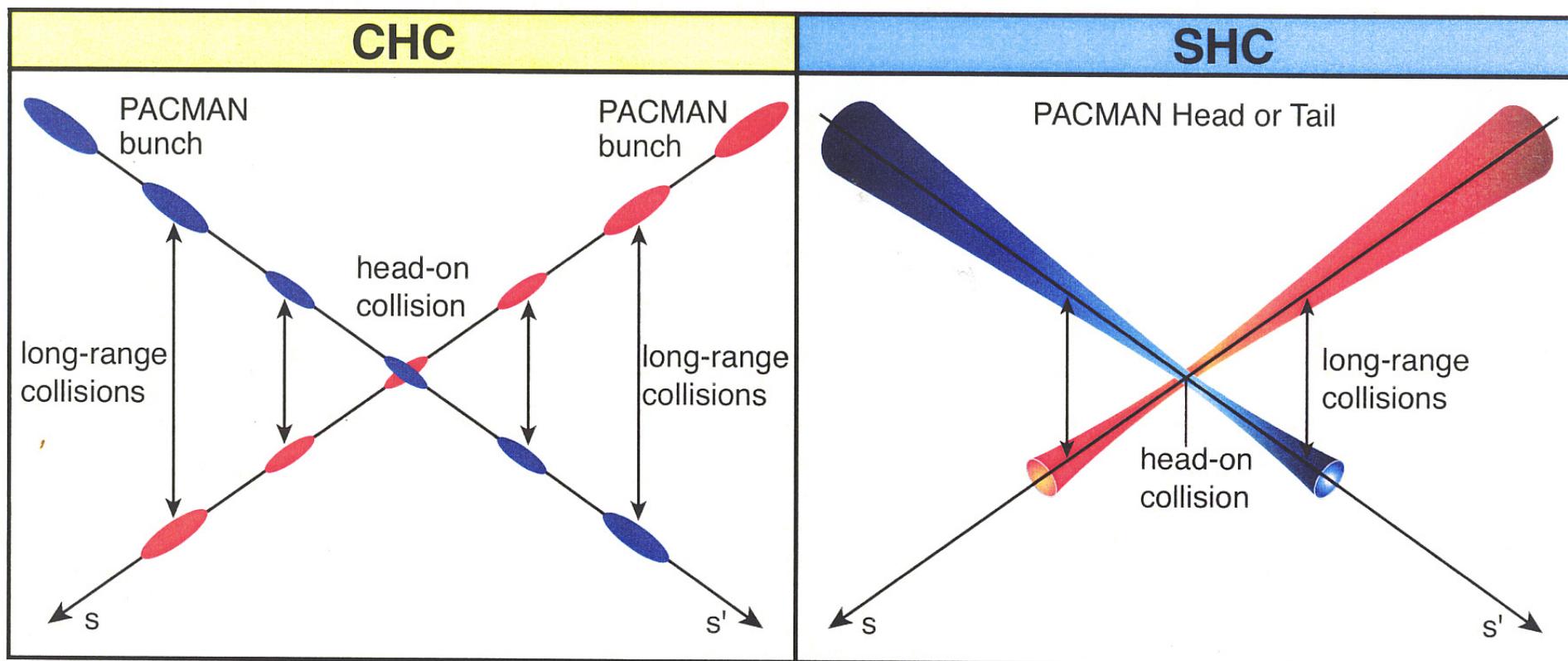
$$F_{CHC}(\Phi') = 1 / \sqrt{1 + (\Phi' \sigma_s / 2\sigma^*)^2}$$

$$F_{SHC}(\Phi, \ell) = \int_0^\ell \frac{\exp\left(-\frac{\gamma \Phi^2 s^2}{2\beta^* \epsilon_n [1 + (s/\beta^*)^2]}\right)}{[1 + (s/\beta^*)^2]} ds$$

LHC-size SHC ($2\ell = 5m$)



PACMAN EFFECTS



	CHC	SHC
Effect		
Abnormal COD		
Abnormal Q_x, Q_y	yes	yes
Abnormal β_x, β_y		
Fraction of PACMAN bunches/particles	15/72 for LHC	mixed in the entire superbunch
Simulation work	done	not yet

Heat Load

Cooling capacity of a vacuum chamber embedded in the super-conducting magnet is limited. **A few W/m.** Heat load originated from circulating beams is serious problem.

Item	remarks	CHC	SHC
Synchrotron radiation	$P = 7.36 \times 10^{-21} \frac{N}{R(m)\rho^2(m)} \left(\frac{E}{mc^2} \right)^4$ <p>simply proportional to N</p>	200mW/m/ring for LHC	Significant for high luminosity operation
Joule-loss due to wall current	<p>Heat power averaged over τ</p> $\bar{P} = \frac{1}{\tau} \int_0^\tau dt \int_V \frac{ i ^2}{\sigma} dx^3$ <p>τ: revolution time i: wall current σ: electric conductivity</p>	70mW/m for LHC	Relatively small because of small magnitude of high frequency components in wall current
Electron cloud * pointed out and estimated by F.Zimmermann	Electrons accelerated in beam-charge potential or induced electric fields proportional to the fall-off in line density hit vacuum chamber	Serious because many short bunches place in the entire ring	much reduced quite few fall-off in line density

Summary

- The SHC scheme seems to be attractive as a possible candidate for LHC upgrade and the future VLHC with an extremely high luminosity.
- In order to convince the high-energy accelerator society of its capability, barrier bucket acceleration must be demonstrated in any existing accelerators as soon as possible.
- How to create a super-bunch by **conventional RF** and **induction devices** should be carefully examined.
- Remained beam physics issues such as **coherent beam-beam effects** and collective instability of a super-bunch must be systematically studied.
- Advantageous and disadvantageous features of the inclined crossing scheme must be evaluated from a more technical point of view and experimental demonstration in a small e^-e^- test-collider is remarkably desired.